

vpgTLE GATE Actor:  
Track-Length Estimator for MC simulations  
of the Prompt-Gamma emission sources in proton therapy

Jean Michel Létang

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Ion Imaging Workshop 2025, Firenze

## Disclaimer

Part of this presentation is based on the work of **Violette Guittet** during her MSc internship at CREATIS, and co-supervised by Étienne Testa.



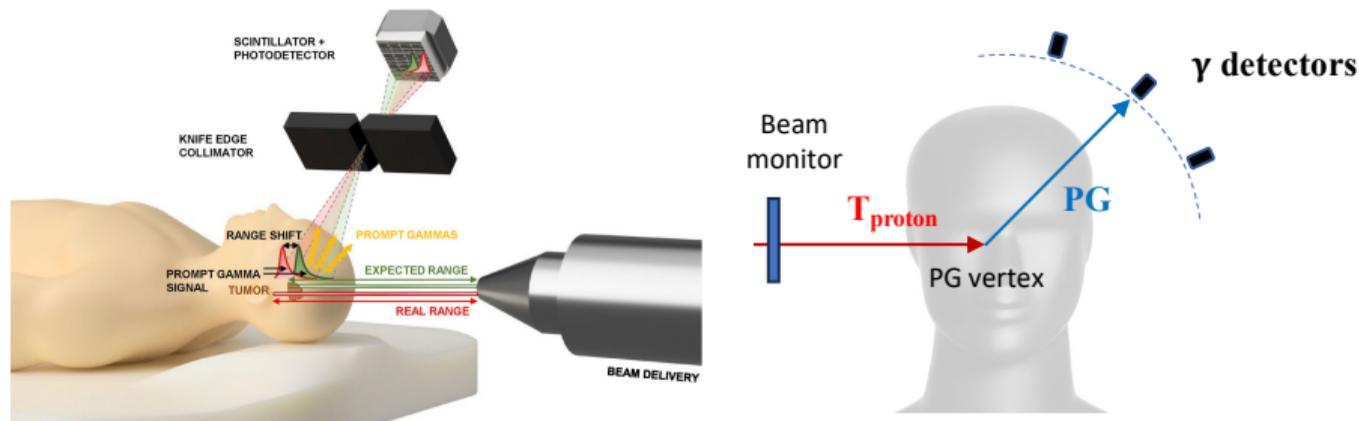
Violette Guittet  
(MSc)



Étienne Testa  
(Associate Professor)

# Radiation therapy

## Range monitoring with Prompt Gamma<sup>3</sup>



⇒ Need of MC simulations to design detection stages:

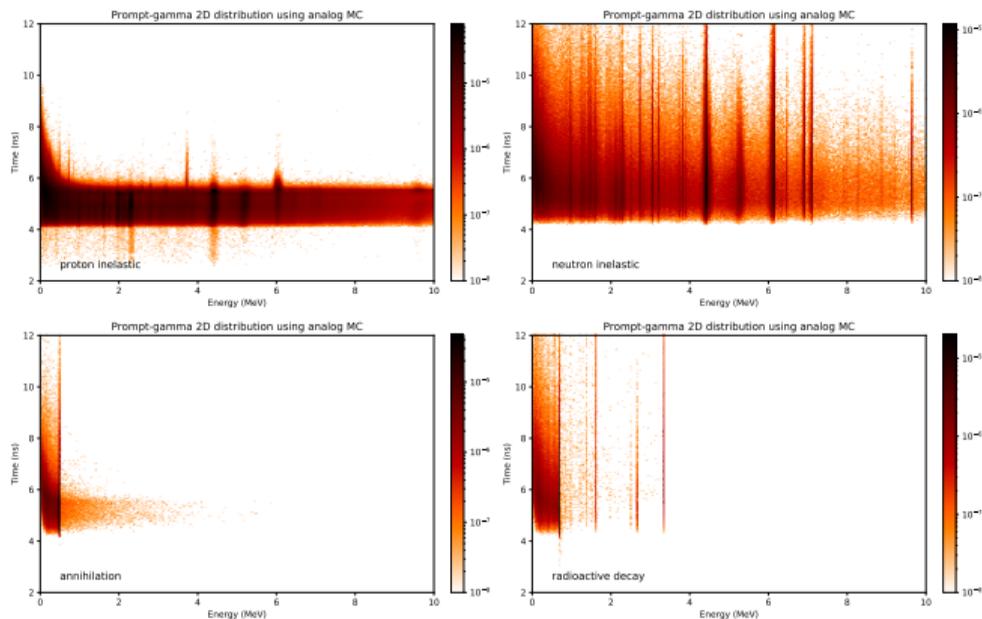
- Prompt-Gamma Time-of-flight Imaging ARrAy (TIARA)<sup>1</sup>,  $\text{PbF}_2$ , 100ps RMS
- Prompt-Gamma Energy Integration (PGEI)<sup>2</sup>,  $\text{PbWO}_4$

<sup>1</sup> M Jacquet et al. "A high sensitivity Cherenkov detector for prompt gamma timing and time imaging". In: [Scientific Reports](#) 13.1 (Mar. 2023). doi: 10.1038/s41598-023-30712-x.

<sup>2</sup> P Everaere et al. "Prompt gamma energy integration: a new method for online-range verification in proton therapy with pulsed-beams". In: [Frontiers in Physics](#) 12 (June 2024). ISSN: 2296-424X. doi: 10.3389/fphy.2024.1371015.

<sup>3</sup> A B Idrissi et al. "First experimental verification of prompt gamma imaging with carbon ion irradiation". In: [Scientific Reports](#) 14.1 (Oct. 2024). ISSN: 2045-2322. doi: 10.1038/s41598-024-72870-6.

## Gamma sources

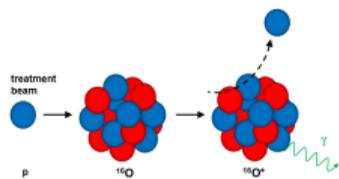
Origins: protontherapy example from H & N treatment plan<sup>4</sup>

⇒ Mainly from **nuclear inelastic** interaction of **proton** and **neutron**

<sup>4</sup>J M Létang, O Allegrini, and É Testa. "Prompt-gamma timing with a track-length estimator in proton therapy". In: *XXth International Conference on the use of Computers in Radiation therapy*. 2024, pp. 584–587.

## Prompt-Gamma sources

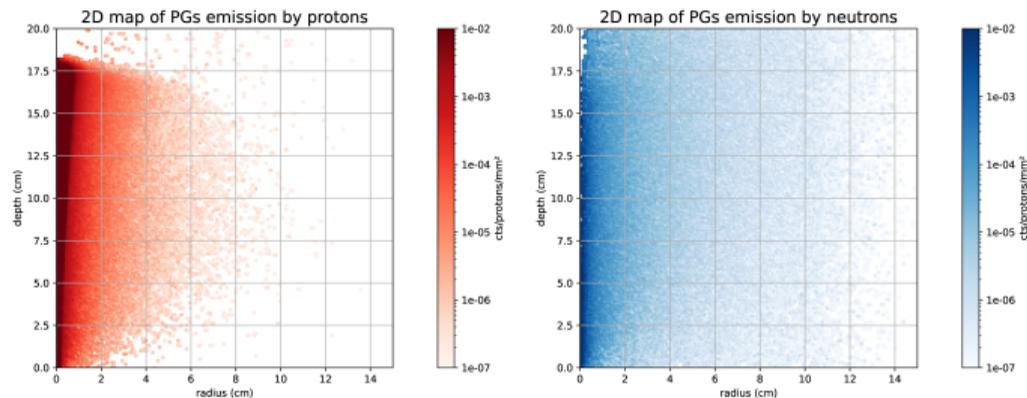
### Protontherapy: Proton vs Neutron<sup>5</sup>



**Nuclear inelastic interaction of proton and neutron**

NB: other projectiles and their product species for hadron therapy with heavier ions (He-, C-ion).

PG spatial distribution (radial slice) with protons at 160MeV in a water tank from **proton** and **neutron**:

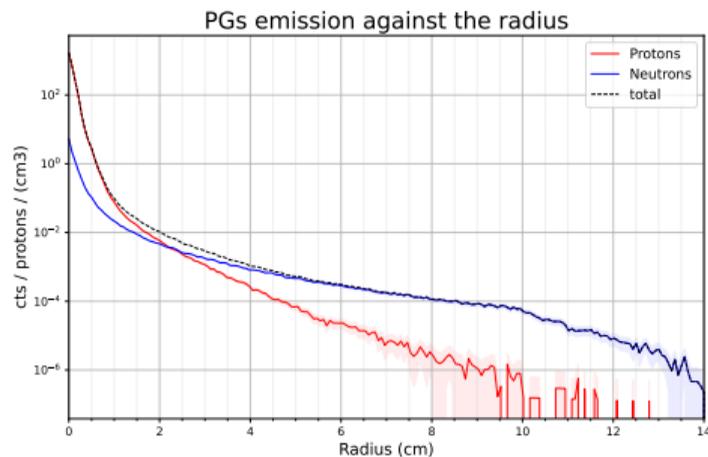
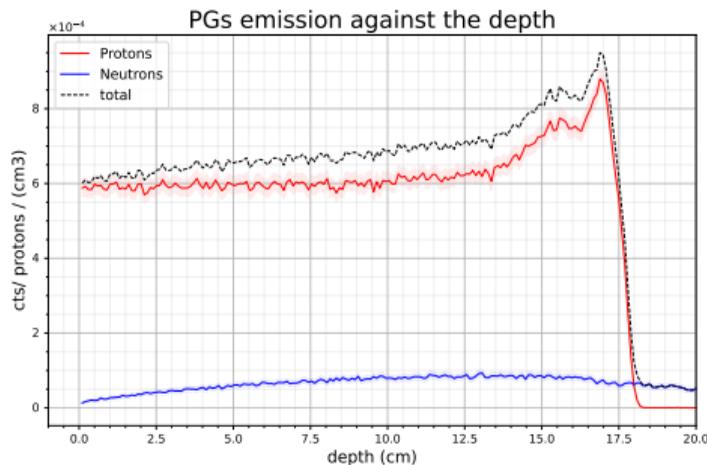


<sup>5</sup>V Guittet. "Extension du module hybride d'émission des rayons  $\gamma$  prompts en protonthérapie dans le code Monte Carlo GATE pour prendre en compte les neutrons secondaires". MSc Report (Med. Phys.) Université de Rennes, 2025.

## Prompt-Gamma sources

### Protontherapy: Proton vs Neutron<sup>6</sup>

Depth (left) and radial (right) PG emission distribution from **proton** and **neutron** in a water tank:



⇒ Neutron-induced PG becomes predominant:

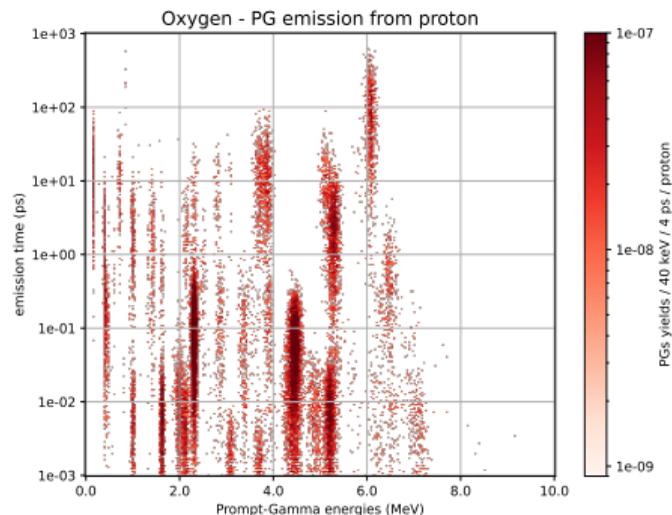
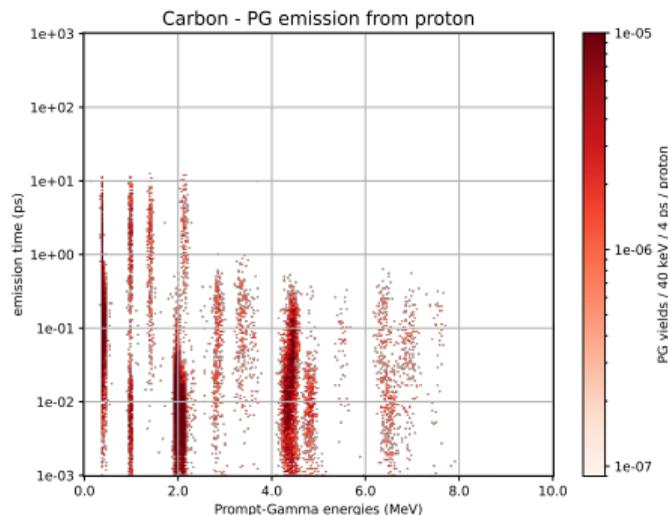
- after the BP along the beam
- and a few cm away from the beam

<sup>6</sup>V Guittet. "Extension du module hybride d'émission des rayons  $\gamma$  prompts en protonthérapie dans le code Monte Carlo GATE pour prendre en compte les neutrons secondaires". MSc Report (Med. Phys.) Université de Rennes, 2025.

# Prompt-Gamma sources

## Decay Promptness<sup>7</sup>

### Nuclear de-excitation gamma-ray lines from proton processes



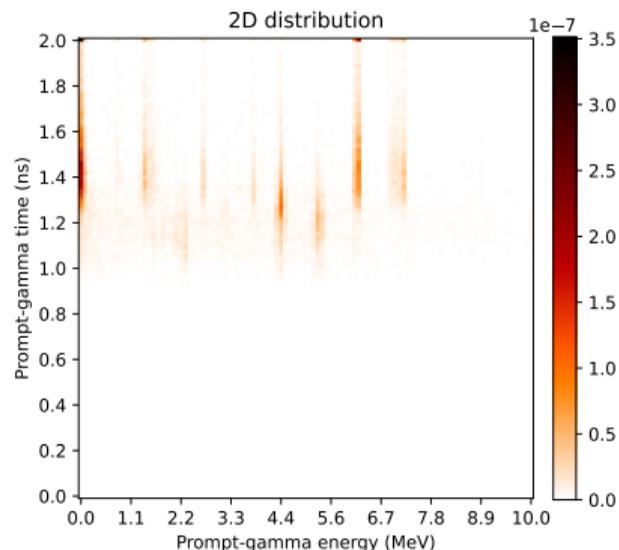
⇒ Negligible decay-time but correlated to gamma-ray energy

<sup>7</sup>V Guittet. "Extension du module hybride d'émission des rayons  $\gamma$  prompts en protonthérapie dans le code Monte Carlo GATE pour prendre en compte les neutrons secondaires". MSc Report (Med. Phys.) Université de Rennes, 2025.

## Prompt-Gamma sources

2D (energy & time) distribution: p@130MeV in water<sup>8</sup>

2D PG yield in a (2mm)<sup>3</sup> voxel at BP depth in water, but 2 cm away from it laterally.



⇒ Is it necessary/possible to store a 2D PG yield distribution at each voxel?

<sup>8</sup>V Guittet. "Extension du module hybride d'émission des rayons  $\gamma$  prompts en protonthérapie dans le code Monte Carlo GATE pour prendre en compte les neutrons secondaires". MSc Report (Med. Phys.) Université de Rennes, 2025.

## Prompt-Gamma sources

### 2D representation: energy & time distribution sampling<sup>9</sup>

#### Prompt-Gamma source sampling:

**space:** 10cm × 10cm × 20cm with a (2mm)<sup>3</sup> sampling: **250 000** voxels

**time:** 10ns time range at 10ps: **1000** time samples

**energy:** 10MeV energy range at 10keV: **1000** energy samples

#### Two solutions:

- **5D** PG distributions at each voxel: 3D space × 1D energy × 1D time:  
→  $250 \times 10^9$  samples at double precision: **2TB** file
- Two **4D** PG distributions at each voxel: 3D space × (1D energy + 1D time):  
→  $2 \times 250 \times 10^6$  samples at double precision: **4GB** file

⇒ Check separability between PG emission time and energy

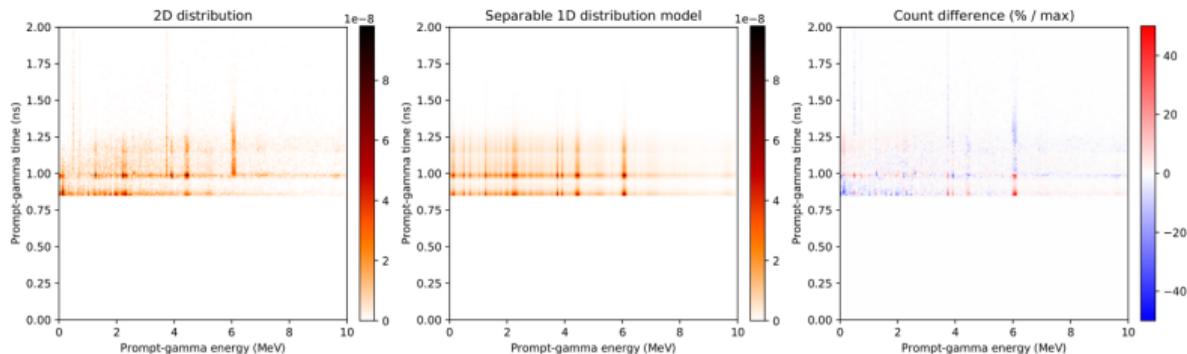
<sup>9</sup>V Guittet. "Extension du module hybride d'émission des rayons  $\gamma$  prompts en protonthérapie dans le code Monte Carlo GATE pour prendre en compte les neutrons secondaires". MSc Report (Med. Phys.) Université de Rennes, 2025.

# Prompt-Gamma sources

## Separability PG emission time vs energy<sup>10</sup>



For a  $(2\text{mm})^3$  bone voxel at 70mm depth:

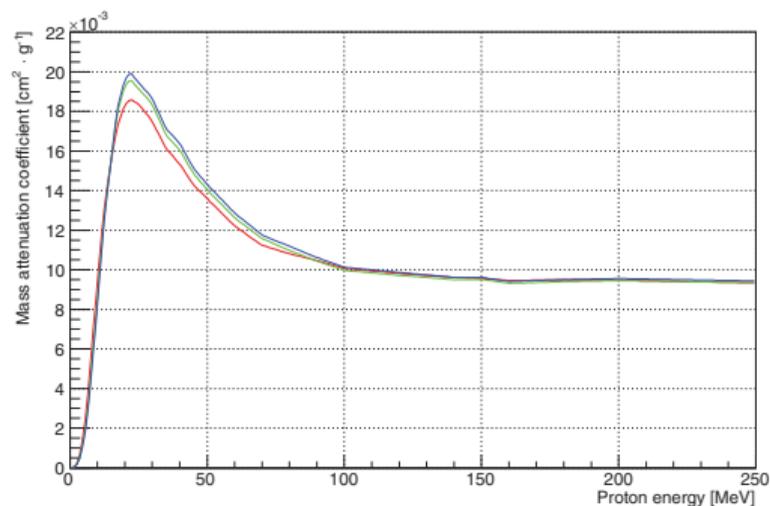


⇒ **Acceptable separability** of PG emission time and energy (except for some  $\gamma$  lines)

<sup>10</sup>J M Létang, O Allegrini, and É Testa. "Prompt-gamma track-length estimator with time tagging from proton tracking". In: *Physics in Medicine and Biology* 69.11 (2024), 115052:1–10. doi: 10.1088/1361-6560/ad4a01.

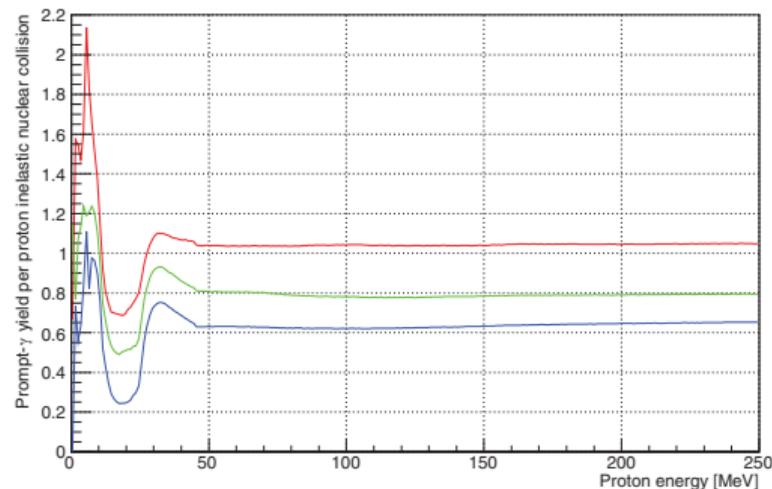
# Monte Carlo simulation

## Computation of the $2 \times 4D$ PG source<sup>11</sup>



Mass attenuation coefficient

Bone – Lung – Muscle



Total PG yield

Bone – Lung – Muscle

1% PG / proton / cm  $\Rightarrow$  Rare event: VRT necessary

<sup>11</sup>W El Kanawati et al. "Monte Carlo simulation of prompt  $\gamma$ -ray emission in proton therapy using a specific track length estimator". In: *Physics in Medicine and Biology* 60.20 (2015), pp. 8067–8086. doi: 10.1088/0031-9155/60/20/8067.

## Sidestep: Dose calculation

### TLE for Kerma approximation<sup>14</sup>

Dose (monoenergetic x-ray beam  $E$ ) at pixel  $\mathbf{x}$ :

$$D(\mathbf{x}) = \underbrace{\Phi(\mathbf{x})}_{\text{Fluence}} \times E \times \underbrace{\mu_{en}(E, \mathbf{x})}_{\rightarrow \text{DataBase}} \times \frac{1}{\rho(\mathbf{x})}$$

where

- the linear energy-absorption coefficient  $\mu_{en}$  must be **computed via MC calculations** (or approximated from NIST database<sup>12</sup>)
- and the particle fluence  $\Phi \equiv$ <sup>13</sup> the total particle path length  $\sum_k L_k$  per volume  $V$

$$\Phi(\mathbf{x}) = \frac{\sum_k L_k(\mathbf{x})}{V(\mathbf{x})}$$

⇒

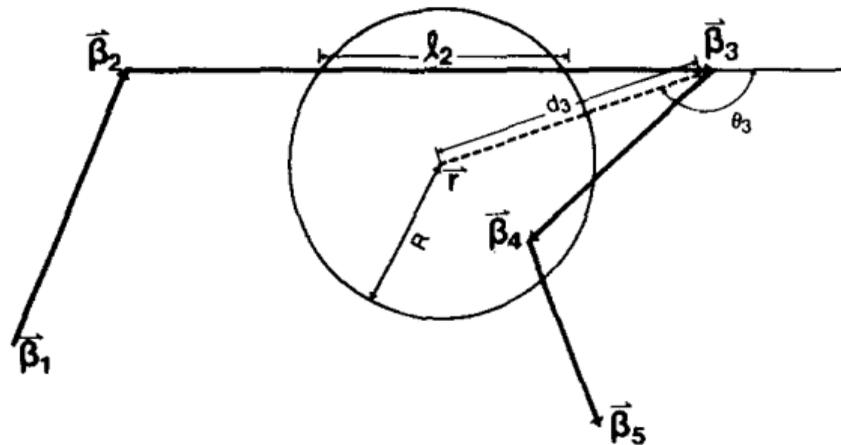
- Linear **Track Length Estimator** (TLE) for fluence
- Need to build a **PG yield database**

<sup>12</sup><https://www.nist.gov/pml/x-ray-mass-attenuation-coefficients>

<sup>13</sup>G A Carlsson. "The dosimetry of ionizing radiation". In: vol. 1. Academic Pr, 1986. Chap. Theoretical Basis for Dosimetry. ISBN: 978-0-12-400401-6.

<sup>14</sup>Jeffrey F Williamson. "Monte Carlo evaluation of kerma at a point for photon transport problems". In: *Medical Physics* 14.4 (1987), pp. 567–576.

## Track-Length Estimator (TLE)

Kerma estimation<sup>15</sup>

- Analog MC: discrete process attached to particle interactions
- TLE: continuous process attached to particle in transportation

<sup>15</sup> Jeffrey F Williamson. "Monte Carlo evaluation of kerma at a point for photon transport problems". In: *Medical Physics* 14.4 (1987), pp. 567–576.

## Track-Length Estimator (TLE)

vpgTLE: voxelized Prompt-Gamma TLE<sup>16</sup>

The TLE variation for Prompt-Gamma energy source computation at voxel  $\mathbf{x}$ :

$$\mathbf{E}_{pg}(\mathbf{x}) = \sum_{i=1}^{N_{\text{steps}}} \sum_{p=1}^{N_{\text{energies}}} L_i(E_p, \mathbf{x}) \times \Gamma_{m(\mathbf{x})}(E_p)$$

where

- $L_i(E_p, \mathbf{x})$  is the length of the step  $i$  in voxel  $\mathbf{x}$  at particle energy  $E_p$ .
- $\Gamma_{m(\mathbf{x})}(E_p)$  is the 1D PG energy distribution per unit length for material  $m(\mathbf{x})$  and particle energy  $E_p$ ,

Nota Bene: the PG database  $\Gamma_m$  is **not scene dependent** and can be built **offline** for each material  $m$  and each particle type (proton, neutron...).

$$\Gamma_m(E_p) = \mathbf{N}_{m,\gamma}(E_p) \frac{\kappa_{m,\text{inel}}(E_p)}{N_{m,\text{inel}}(E_p)}$$

<sup>16</sup>W El Kanawati et al. "Monte Carlo simulation of prompt  $\gamma$ -ray emission in proton therapy using a specific track length estimator". In: *Physics in Medicine and Biology* 60.20 (2015), pp. 8067–8086. doi: 10.1088/0031-9155/60/20/8067.

## vpgTLE

PG database  $\Gamma_{m(x)}(E_p)$ : error analysis<sup>17</sup>

$$E_{pg}(\mathbf{x}) = \sum_{i=1}^{N_{\text{steps}}} \sum_{p=1}^{N_{\text{energies}}} L_i(E_p, \mathbf{x}) \times \Gamma_{m(x)}(E_p)$$

Error types and sources: $L_i(E_j, \mathbf{x})$ : **statistical** error

$$\text{statistical relative variance} \propto \frac{\sigma^2(L(\mathbf{x}))}{n(\mathbf{x}) \bar{L}_n^2(\mathbf{x})}$$

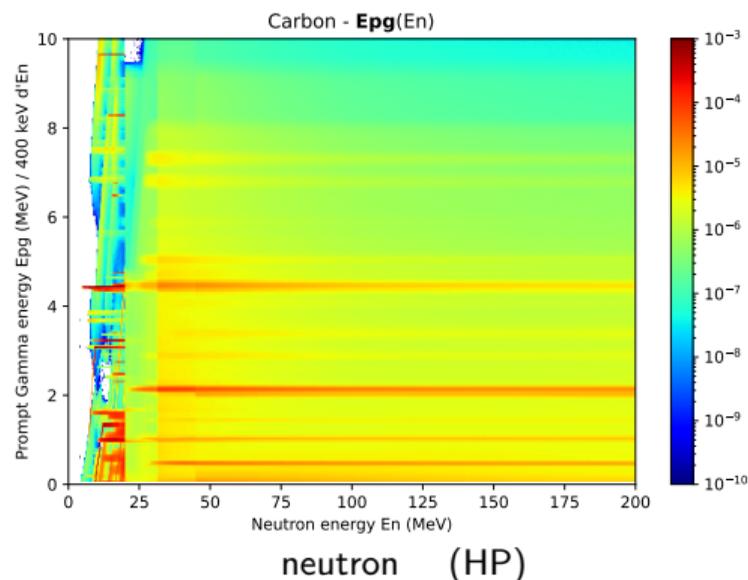
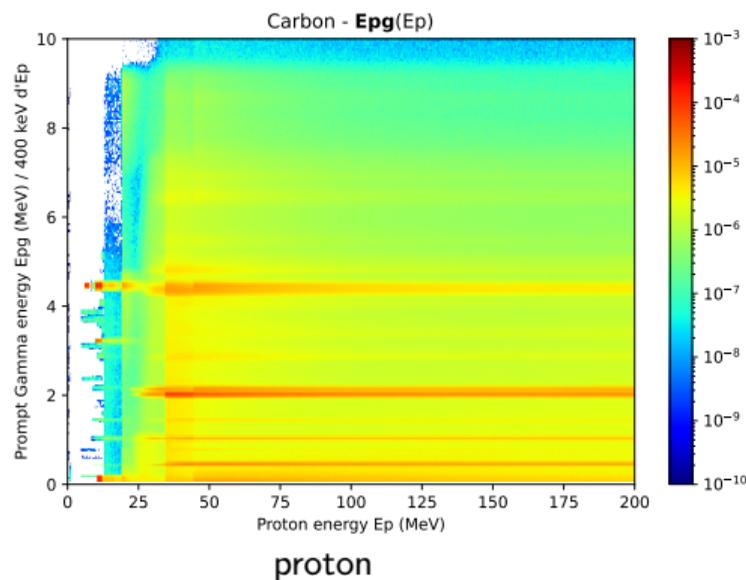
 $\Rightarrow$  fast convergence (on the primary particle track), **low stat** sufficient $\Gamma_{m(x)}(E_j)$ : **systematic** error

$$\text{systematic relative variance} \propto \frac{1}{N_{m(x),\gamma}(E_p, E_\gamma)}$$

with  $N_{m(x)}(E_p, E_\gamma)$  the nr of PG scored for particle energy  $E_p$  in the PG energy bin  $E_\gamma$  for material  $m(x) \Rightarrow$  **high stat** required.

<sup>17</sup>W El Kanawati et al. "Monte Carlo simulation of prompt  $\gamma$ -ray emission in proton therapy using a specific track length estimator". In: *Physics in Medicine and Biology* 60.20 (2015), pp. 8067–8086. doi: 10.1088/0031-9155/60/20/8067.

## vpgTLE

PG database  $\Gamma_{m(x)}(E_p)$ : examples<sup>18</sup>

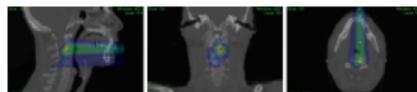
Each column of  $\Gamma_{m(x)}(E_p)$  (indexed by the particle energy  $E_p$ ) is the 1D PG-energy emission yield.  
 ⇒ Root file format (JSON too large)

<sup>18</sup>V Guittet. "Extension du module hybride d'émission des rayons  $\gamma$  prompts en protonthérapie dans le code Monte Carlo GATE pour prendre en compte les neutrons secondaires". MSc Report (Med. Phys.) Université de Rennes, 2025.

## vpgTLE

PG source calculation: online protocol<sup>19</sup>

For a given scene: (eg from a TPS)

Computation of the two 4D PG yield sources: At **each step**  $i$ **Energy:** Increment the 1D PG energy distribution at voxel  $\mathbf{x}$  with

$$E_{pg}(\mathbf{x}) += L_i(E_p, \mathbf{x}) \times \Gamma_{m(\mathbf{x})}(E_p)$$

where  $E_p$  is the particle energy, sampled randomly along its step.**Time:** Increment 1 sample of the 1D PG time distribution at voxel  $\mathbf{x}$  with

$$t_{pg}(\mathbf{x}, t_p) += L_i(E_p, \mathbf{x}) \times \left( \sum_{E_{pg}} \Gamma_{m(\mathbf{x})}(E_p, E_{pg}) \right)$$

where  $t_p$  is the **particle** time, sampled randomly along its step.

(⇒ Nuclear de-excitation time neglected)

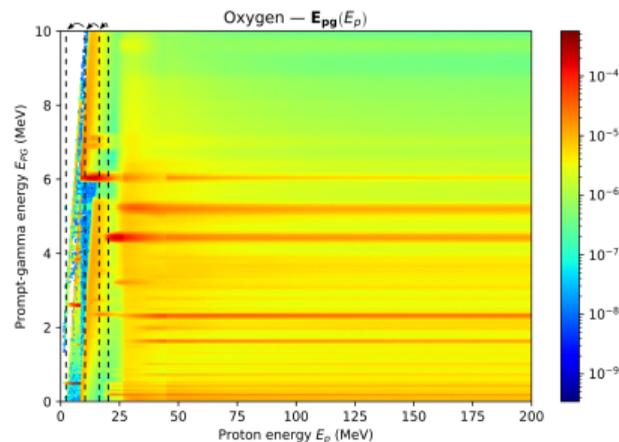
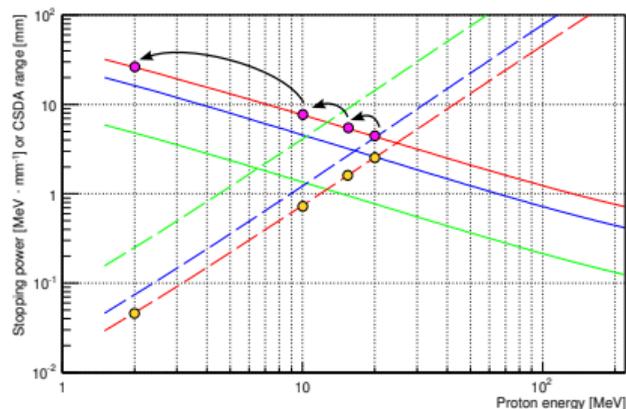
<sup>19</sup>W El Kanawati et al. "Monte Carlo simulation of prompt  $\gamma$ -ray emission in proton therapy using a specific track length estimator". In: *Physics in Medicine and Biology* 60.20 (2015), pp. 8067–8086. doi: 10.1088/0031-9155/60/20/8067.

## vpgTLE

Aliasing in PG database reading<sup>20</sup>

With a 1mm-step for protons at 20MeV in bone:

- $dE/dx(p@20\text{MeV}) = 4.5 \text{ MeV/mm}$ ,
- $\text{CSDA}(p@20\text{MeV}) = 2.5 \text{ mm in bone}$ .



SP (solid) and CSDA (dashed) for **bone**, **muscle** and **lung**

PG database  $\Gamma_{\text{oxygen}}(E_p)$  (45% in bone)

⇒ Discontinuities in PG production: possible **aliasing** in DB reading:  $\Delta$  step limiter).

<sup>20</sup>W El Kanawati et al. "Monte Carlo simulation of prompt  $\gamma$ -ray emission in proton therapy using a specific track length estimator". In: *Physics in Medicine and Biology* 60.20 (2015), pp. 8067–8086. doi: 10.1088/0031-9155/60/20/8067.

## vpgELE

Energy-Loss variant<sup>21</sup>

Instead of the standard vpgTLE

$$\mathbf{E}_{\text{pg}}(\mathbf{x}) \doteq \int_{r=r_{\text{in}}(\mathbf{x})}^{r_{\text{out}}(\mathbf{x})} \Gamma_{\text{m}(\mathbf{x})}(E_p(r)) dr$$

an Energy-Loss Estimator can be derived (vpgELE)

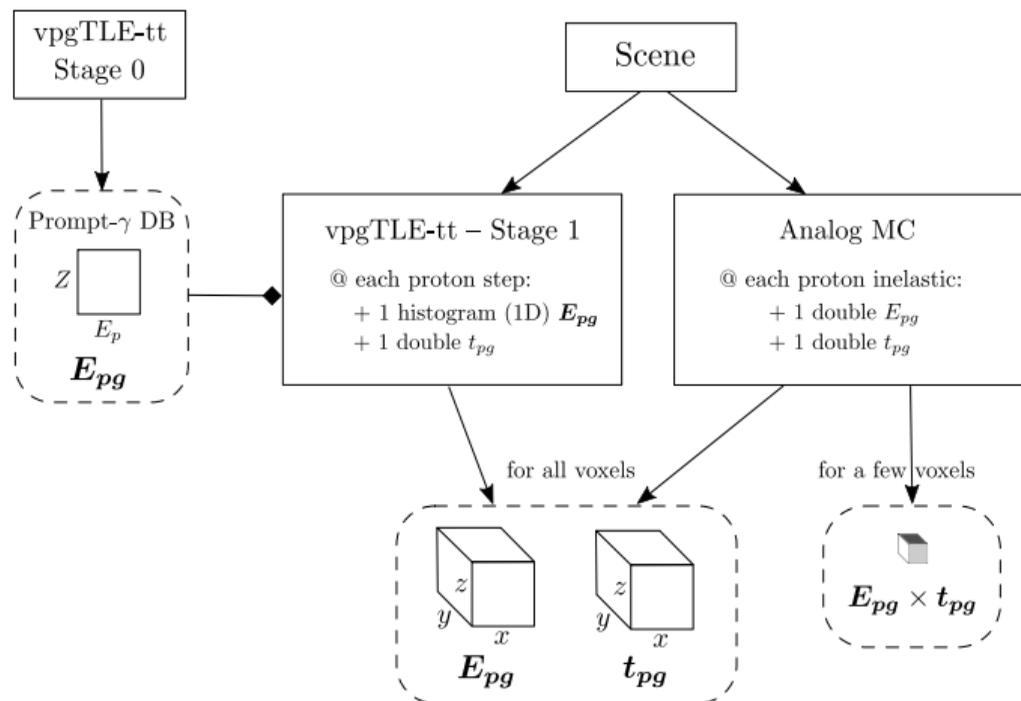
$$\mathbf{E}_{\text{pg}}(\mathbf{x}) \doteq \int_{E_p=E_{\text{in}}(\mathbf{x})}^{E_{\text{out}}(\mathbf{x})} \frac{\Gamma_{\text{m}(\mathbf{x})}(E_p)}{S(E_p)} dE_p$$

where  $S(E_p)$  is the stopping power of the incident particle.

⇒ Another **cumulative** PG database could be introduced to tackle energy aliasing with this new estimator **vpgELE**.

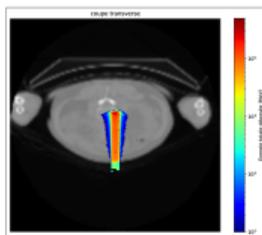
<sup>21</sup>W El Kanawati et al. "Monte Carlo simulation of prompt  $\gamma$ -ray emission in proton therapy using a specific track length estimator". In: *Physics in Medicine and Biology* 60.20 (2015), pp. 8067–8086. doi: 10.1088/0031-9155/60/20/8067.

# vpgTLE Diagram<sup>22</sup>

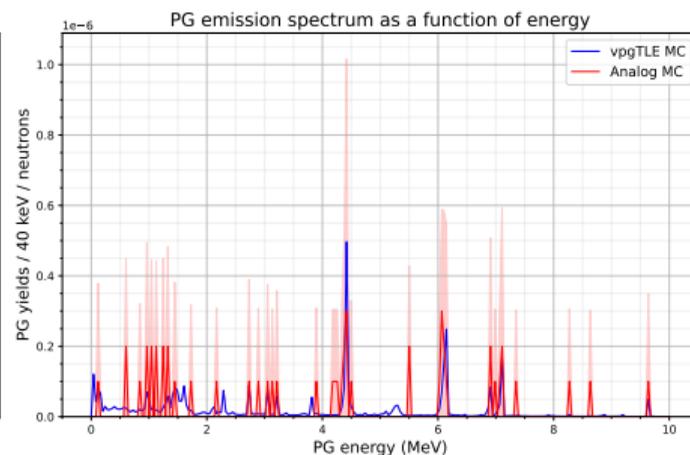
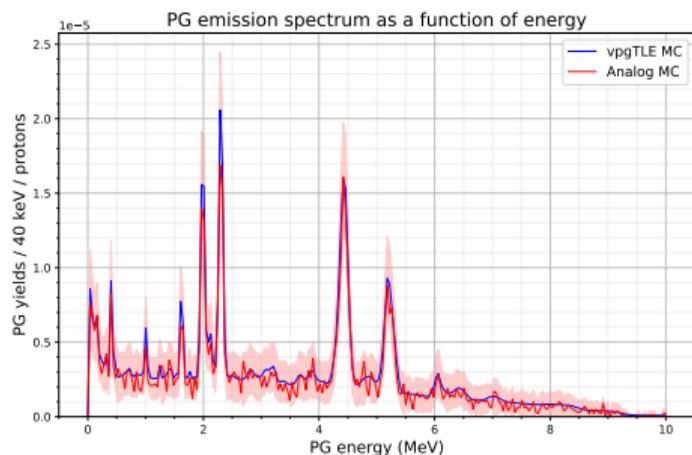


<sup>22</sup>J M Létang, O Allegrini, and É Testa. "Prompt-gamma track-length estimator with time tagging from proton tracking". In: *Physics in Medicine and Biology* 69.11 (2024), 115052:1–10. doi: 10.1088/1361-6560/ad4a01.

## vpgTLE

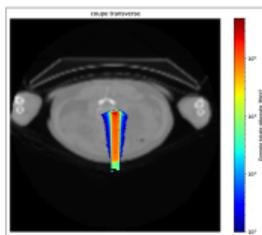
PG energy distribution at VOI (Gate 10): proton vs neutron<sup>23</sup>

- Beam: proton@130MeV
- VOI: (4mm)<sup>3</sup> voxel
- Stats: 10<sup>6</sup> vpgTLE vs 10<sup>7</sup> analog MC

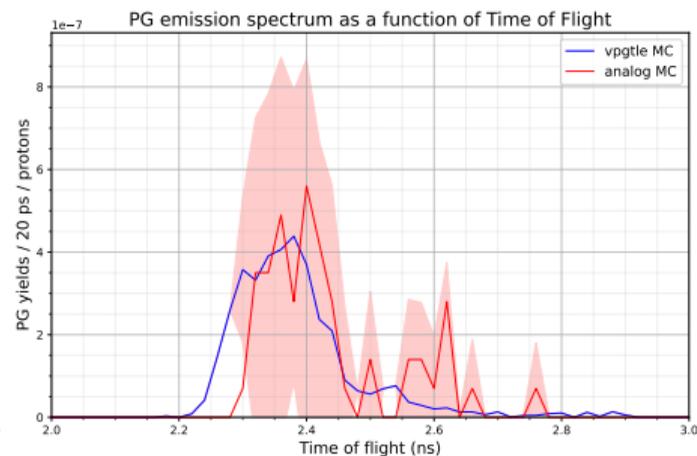
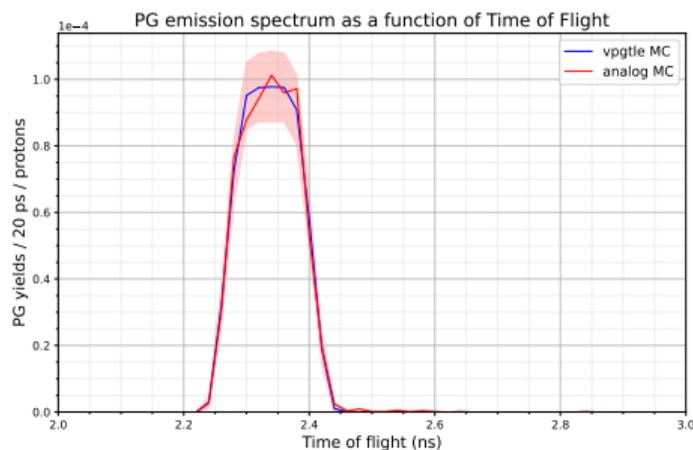


<sup>23</sup>V Guittet. "Extension du module hybride d'émission des rayons  $\gamma$  prompts en protonthérapie dans le code Monte Carlo GATE pour prendre en compte les neutrons secondaires". MSc Report (Med. Phys.) Université de Rennes, 2025.

## vpgTLE

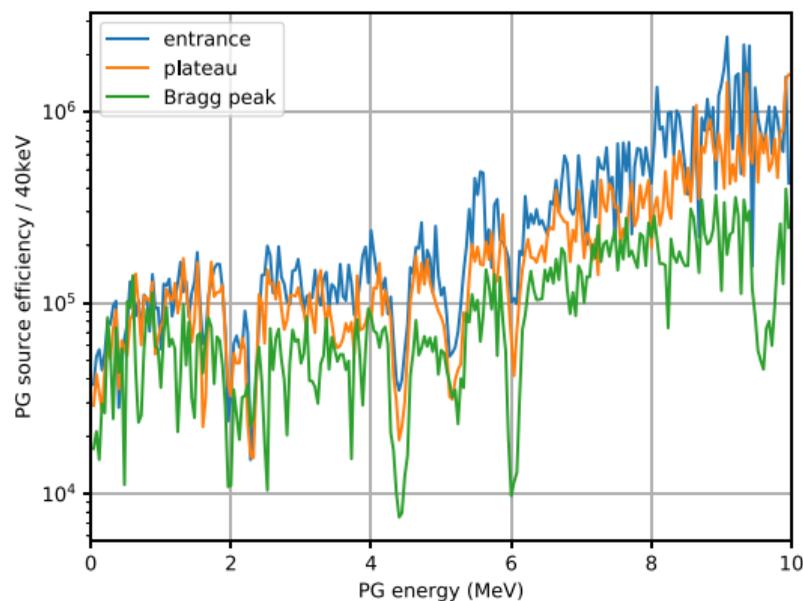
PG time distribution at VOI (Gate 10): proton vs neutron<sup>24</sup>

- Beam: proton@130MeV
- VOI: (4mm)<sup>3</sup> voxel
- Stats: 10<sup>6</sup> vpgTLE vs 10<sup>7</sup> analog MC



<sup>24</sup>V Guittet. "Extension du module hybride d'émission des rayons  $\gamma$  prompts en protonthérapie dans le code Monte Carlo GATE pour prendre en compte les neutrons secondaires". MSc Report (Med. Phys.) Université de Rennes, 2025.

## vpgTLE

Efficiency gain wrt Analog MC (Gate 9.4)<sup>25</sup>

⇒ Efficiency gain wrt Analog MC of about  $10^5$ :  $\frac{1}{1\% \text{ PG/cm}} \times 5 \text{ voxels/cm} \times 10^3 \text{ PG energy bins} = 5 \times 10^5$

<sup>25</sup>J M Létang, O Allegrini, and É Testa. "Prompt-gamma track-length estimator with time tagging from proton tracking". In: *Physics in Medicine and Biology* 69.11 (2024), 115052:1–10. doi: 10.1088/1361-6560/ad4a01.

## Conclusions

### Achievements:

- vpgTLE ported to Gate 10
- expansion to neutron

### To be done:

- implement vpgTLE ( $2 \times 4D$ ) PG source in Gate 10
- extend to heavier ions (He, C)
- improve PG database construction (compatibility with *G4 Physics List Builder*)
- implement vpgELE (Energy-Loss Estimator)

