

Material Budget Imaging

Potential, limits and applications

Paul Schütze, Hendrik Jansen



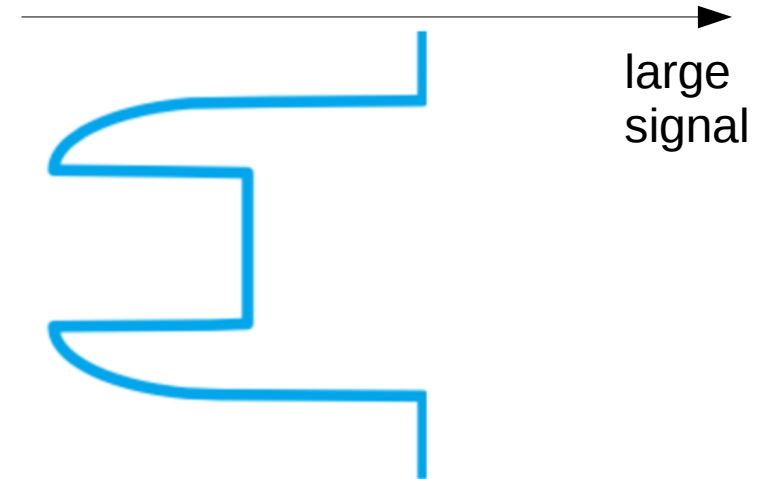
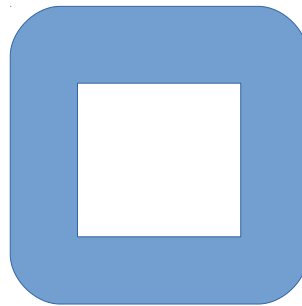
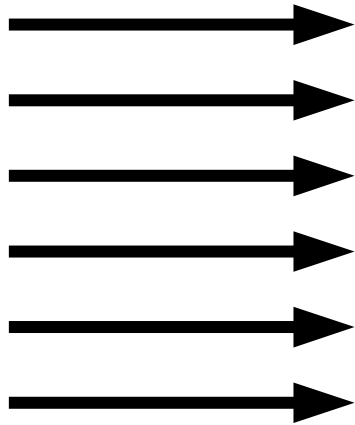
Imaging in a



Probe
- x-ray, neutron

Interaction with the target
- absorption

Measure physical quantity
- intensity



Imaging in a



Probe

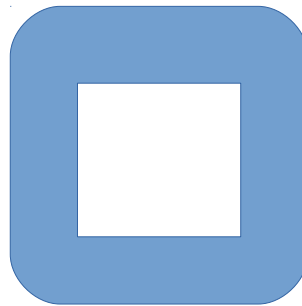
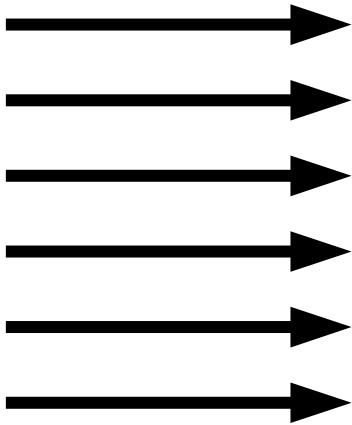
- x-ray, neutron
- **charged particle**

Interaction with the target

- absorption
- energy loss
- **scattering**

Measure physical quantity

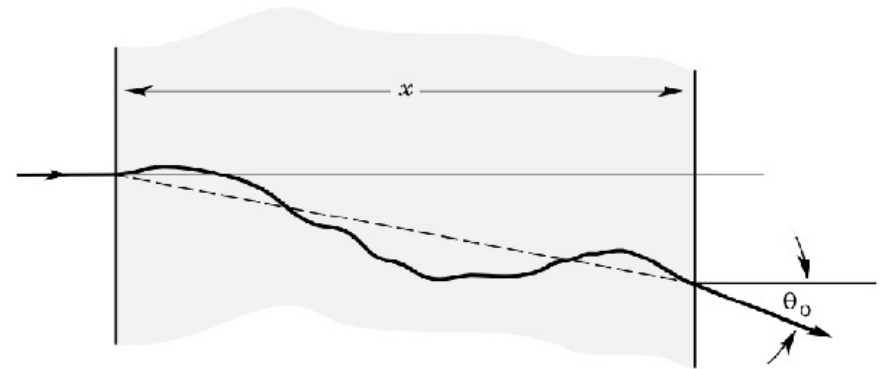
- intensity
- energy loss (ΔE)
- **variance of deflection angle**



Physics of Material Budget Imaging

- High-energy particle undergoes multiple Coulomb scattering when traversing material
 - Particle is deflected
- Scattering angle distribution:
Gaussian-like centre with tails at larger angles
- The Gaussian width predicted by **Highland**

$$\Theta_0 = \left(\frac{13.6 \text{ MeV}}{\beta c p} \cdot z \right) \cdot \sqrt{\varepsilon} \cdot (1 + 0.038 \ln \varepsilon)$$



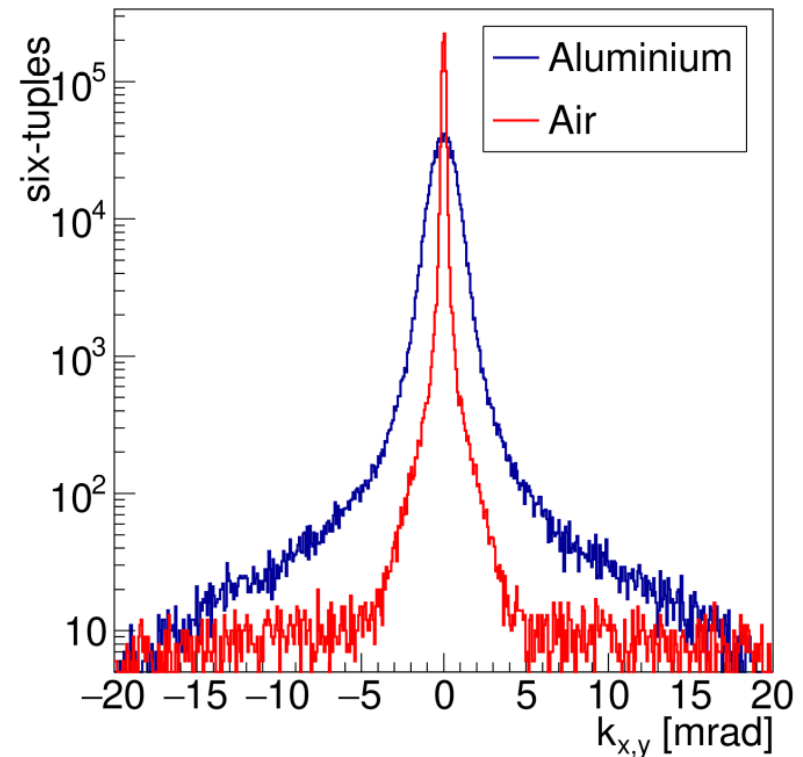
Material Budget: $\varepsilon = x/X_0$

x : Path length in the material

X_0 : Material's radiation length

(e- loses all but 1/e-th of its energy)

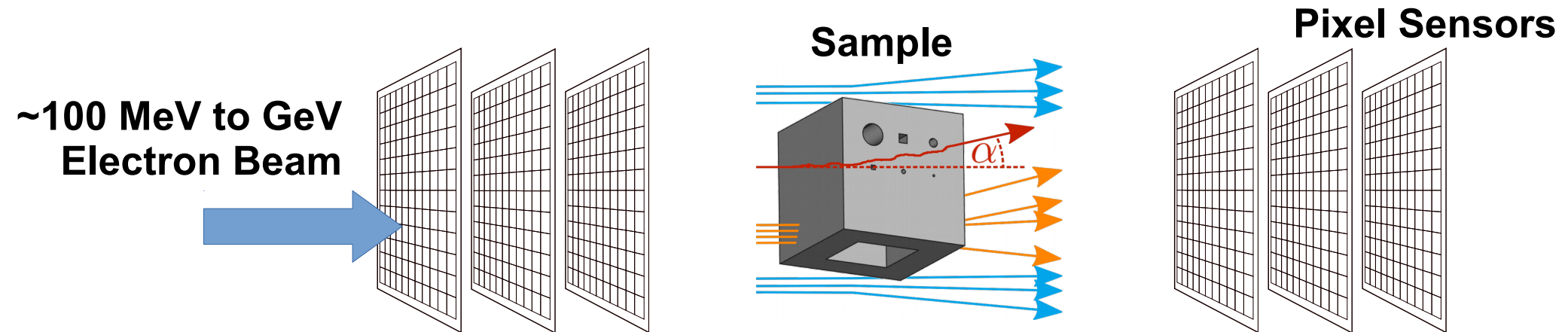
- Measurement:
Scattering angle distribution
- Characteristic quantity:
Material budget



Material Budget Imaging

Imaging method based on multiple scattering

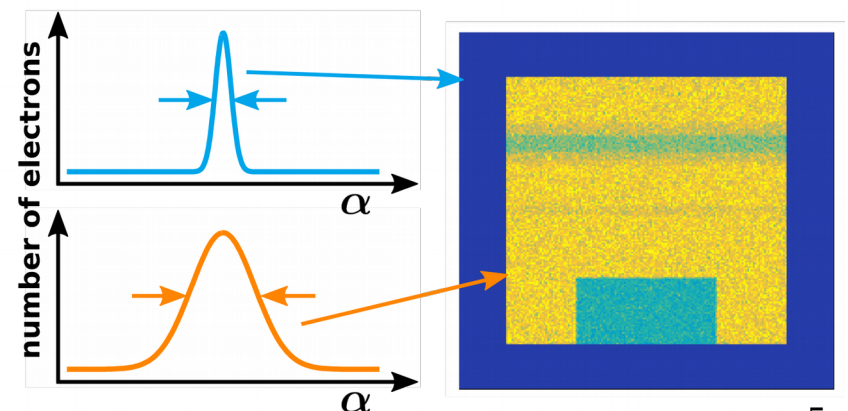
→ Measure each trajectory (in front and behind sample!)



→ Group electrons into pixels at virtual plane through sample

→ Calculate width of angular distribution per pixel

→ Repeat for all projections and perform backprojection



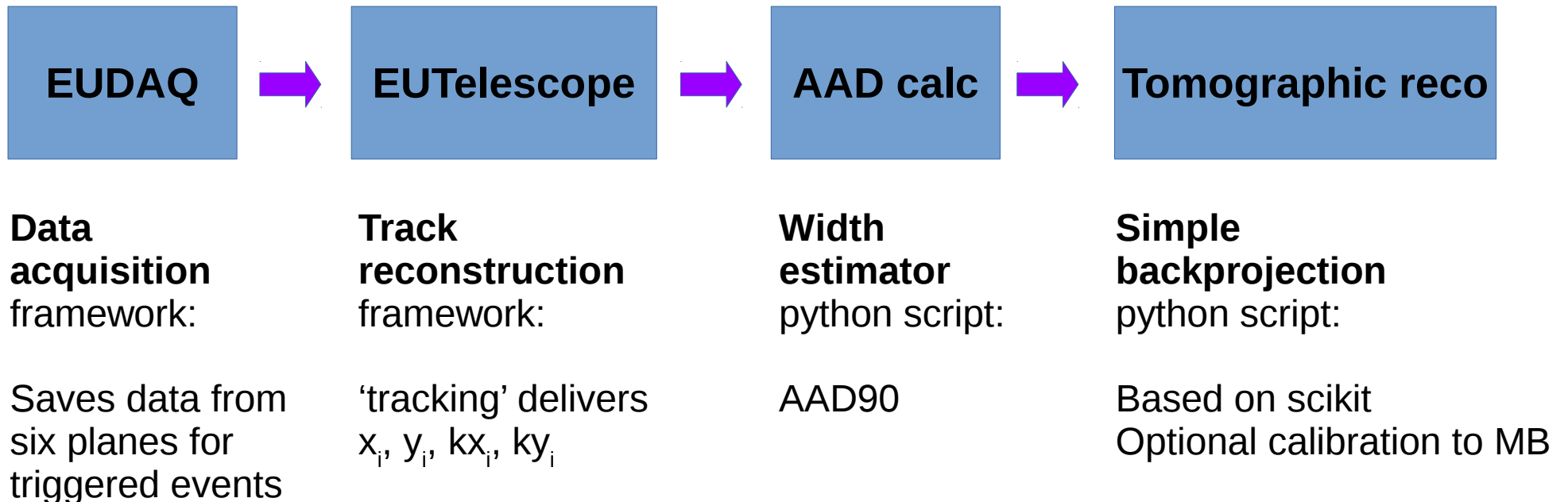
EUDET Beam Telescopes

- 6 sensors: Mimosa 26
 - Pixel Pitch: $18.4\ \mu\text{m} \times 18.4\ \mu\text{m}$
 - Active area: $10.6\ \text{mm} \times 21.2\ \text{mm}$
 - Intrinsic sensor resolution: $> 3.24\ \mu\text{m}$
- 4 PMTs as coincidence trigger
- Track resolution at sample: $\sigma = 2 - 10\ \mu\text{m}$
- *AllPix* Detector Simulation Framework (based on *Geant4* libraries)
 - Simulation of the particle propagation
 - Simulation of detector response
 - Data processing via exact same chain as with data



Reconstruction chain

From data taking to tomographic images



Track reco and width estimation

General Broken Lines (GBL) for track fitting

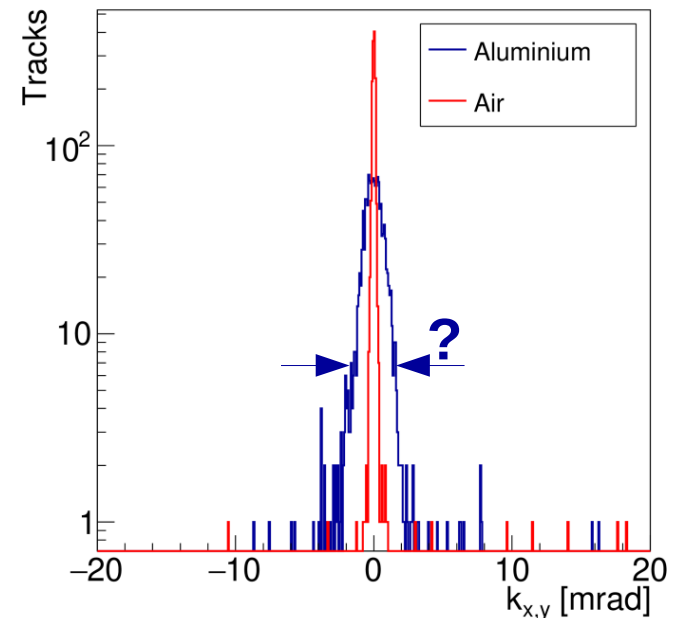
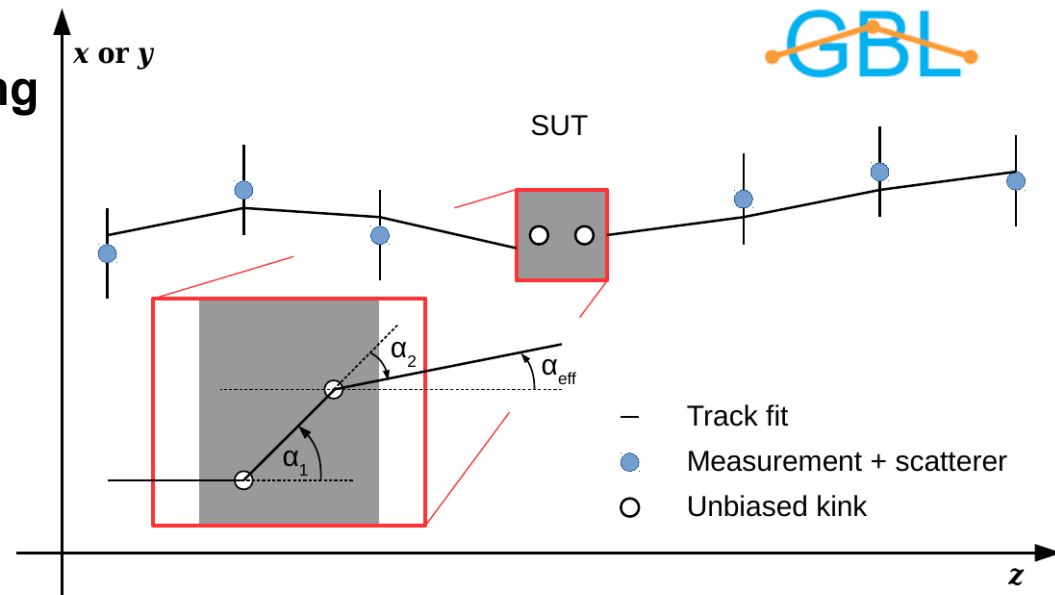
- Find the most probable trajectory based on the measured hits
- Includes known MB at planes
- Introduces unbiased kink at the sample

Method for width estimation

- Calculate *Average Absolute Deviation* of the inner 90% quantile
- Best performance out of 11 tested fitting and statistical methods
- Conversion to MB via Highland formula or via calibration

Challenges

- Non-Gaussian tails of the distribution
- Low statistics



Calibration

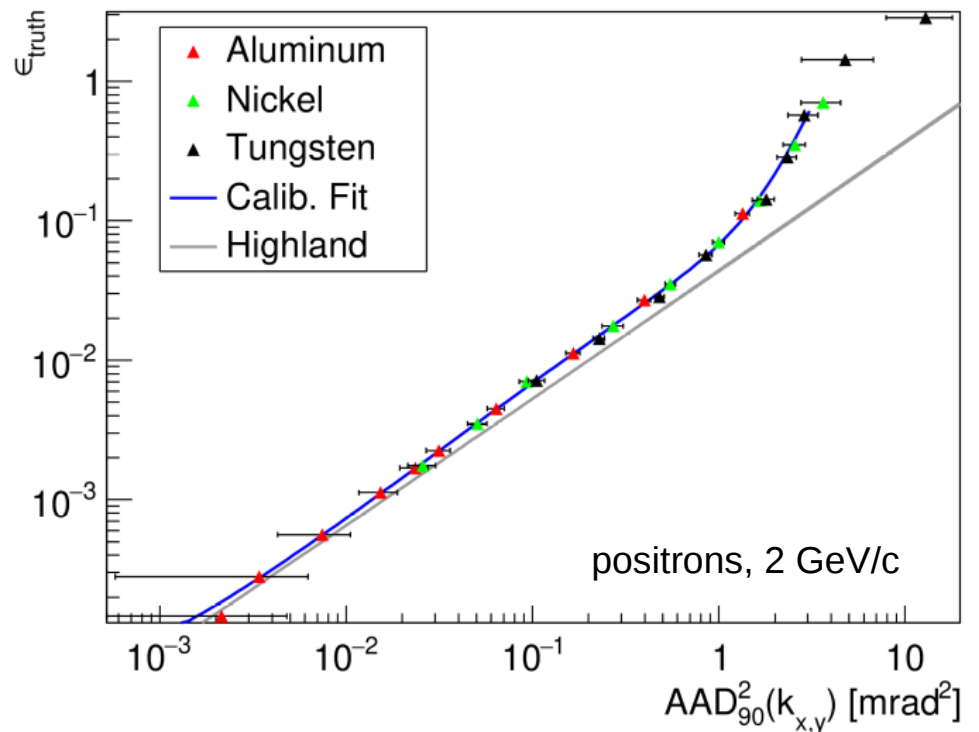
Calculation of the Material Budget from scattering width

- Inverting the Highland formula for a determination of the material budget leads to discrepancies to expected values

$$\Theta_0 = \left(\frac{13.6 \text{ MeV}}{\beta c p} \cdot z \right) \cdot \sqrt{\varepsilon} \cdot (1 + 0.038 \ln \varepsilon)$$

Acquiring calibration curves

- Measure the angle distribution for known scatterers
- Metal foils from 13 μm of aluminum to 2 cm of tungsten
→ $\text{AAD}_{90}(\varepsilon; E)$
- Invert fit to data for the calibration of unknown samples
→ $\varepsilon(\text{AAD}_{90}; E)$



Why MBI?

Considerable interest and potential in MBI

- Various **LHC upgrade activities** in particle physics
 - Estimate of 2D MB distribution for realistic detector description
- **Non-destructive testing** of prototypes
 - e.g. batteries, high-Z material
- **Medical imaging/treatment planning**
 - possible dose advantage
 - possibly less artefacts

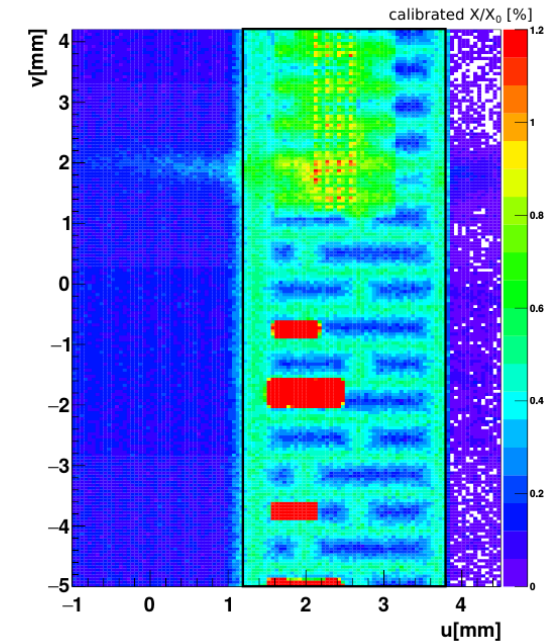
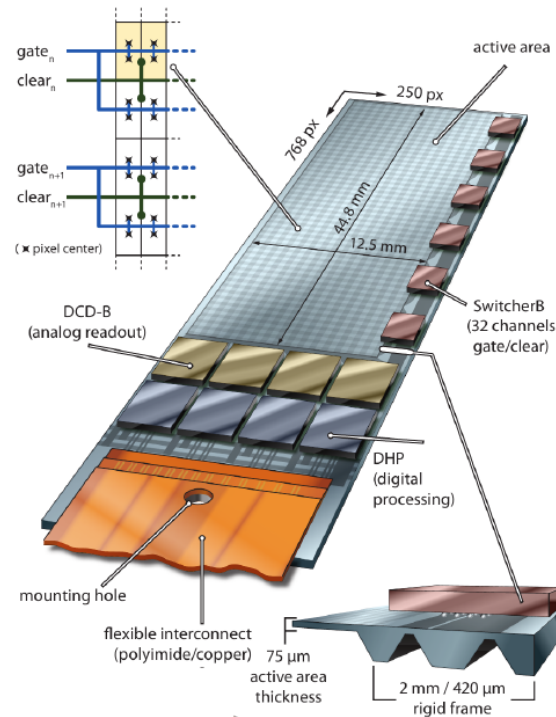
Measure 200 to 2000 projections
→ Need **high rates**

Seamless image/no stitching
→ Need **large area** beam + detector

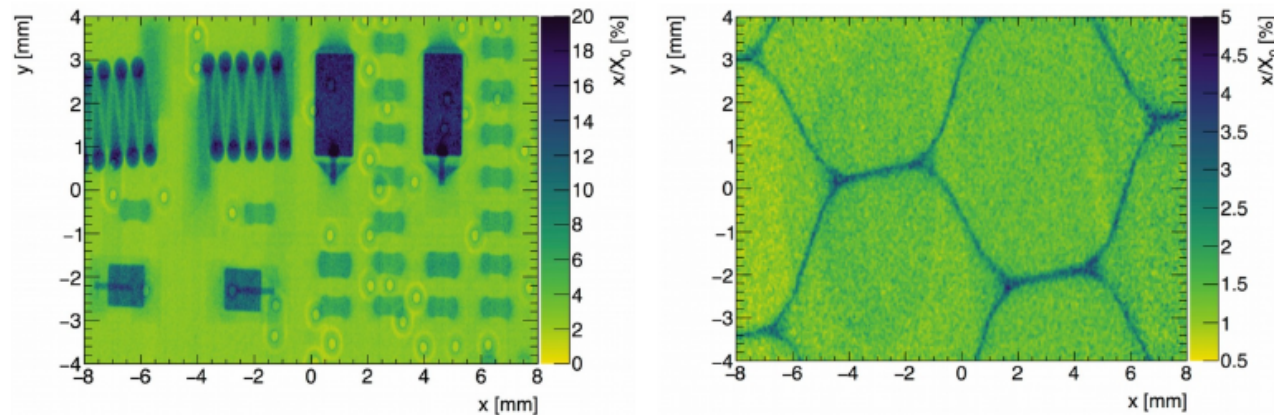


MBI at Belle II / ATLAS

Belle II PXD module



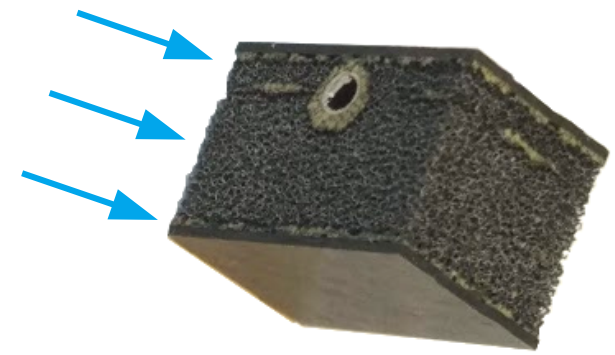
ATLAS Tracker endcap petal



U. Stolzenberg et al.

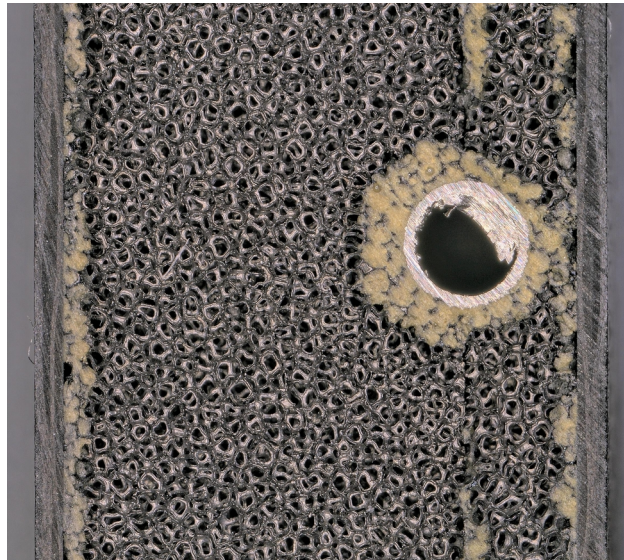
M. Queitsch-Maitland et al.

Results of 2D MBI

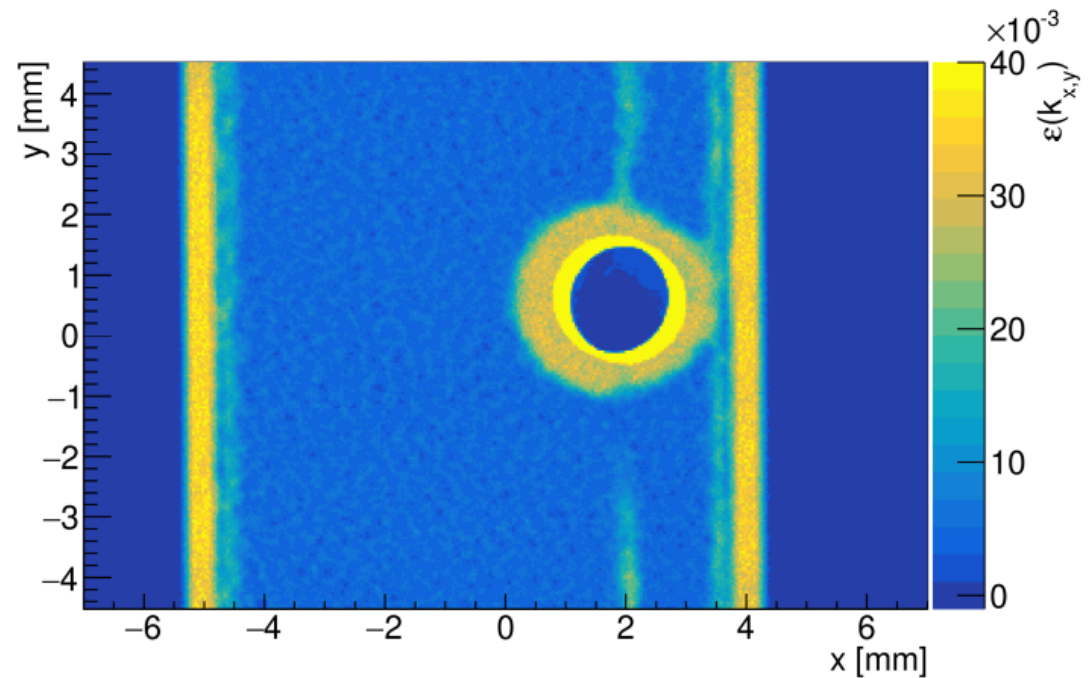


CMS Tracker Support Structure Prototype

- Carbon Foam / CFRP plates / Cooling pipe / Glue
- Qualitative analysis
- Quantitative analysis



Microscope Image



Material Budget Image

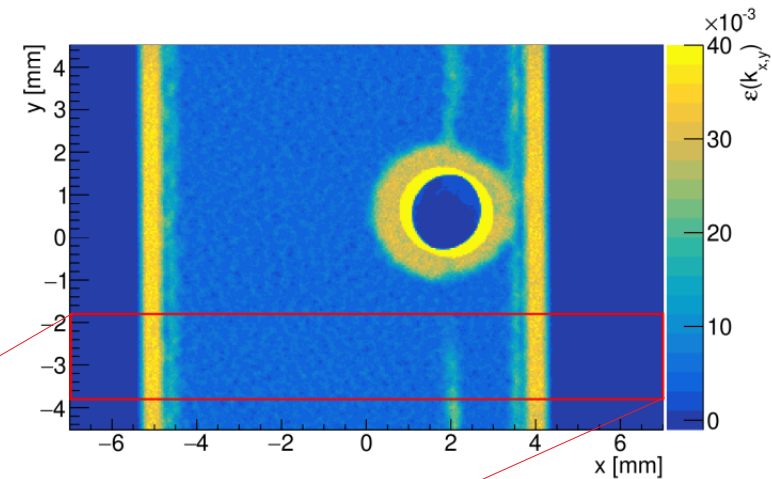
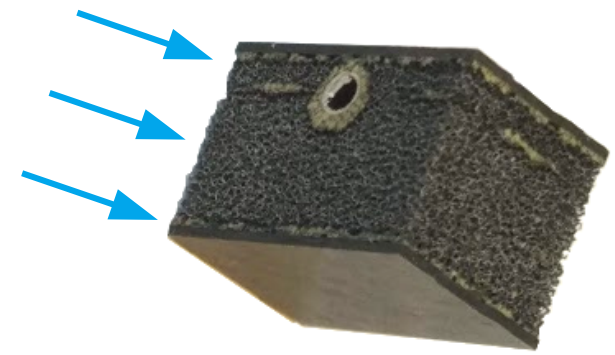
Results of 2D MBI

Qualitative Analysis

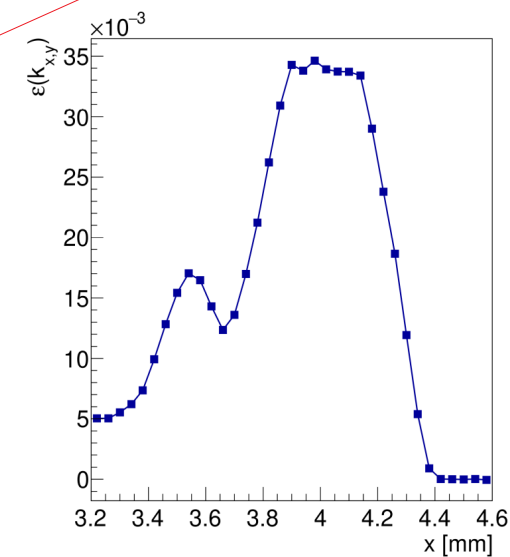
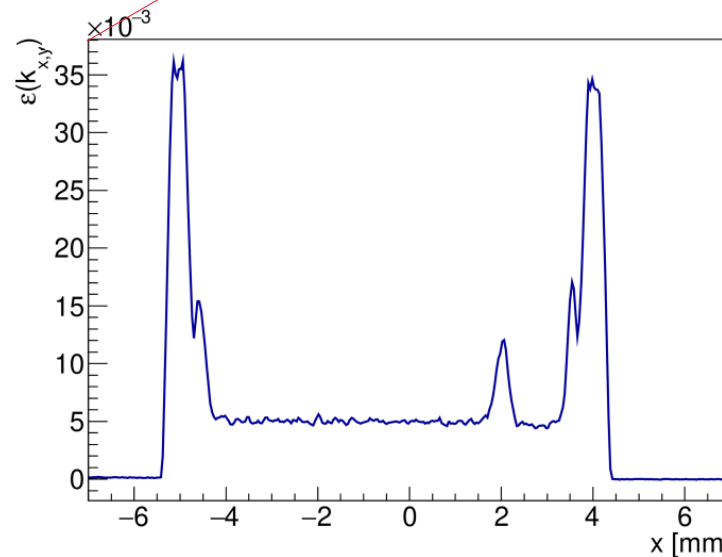
- E.g. investigate glue distribution

Quantitative Analysis

- Measure the actual material budget or radiation length of the sample



X_0 [mm]	Prediction	MBI
Carbon foam	2247 $\pm 10\%$	1930 ± 360 (std)
CFRP	264 $\pm 10\%$	274 ± 17 (std)
Water	360.8	soon!

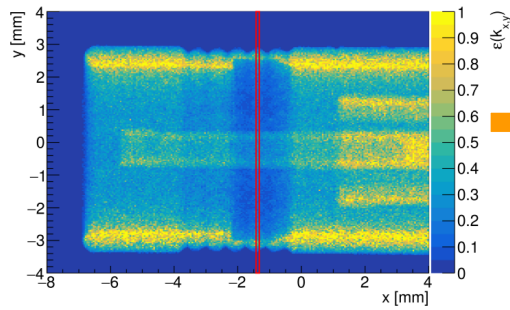


Examples of 3D MBI

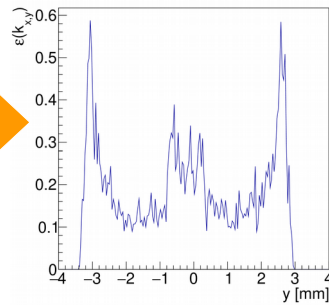


Reconstruction

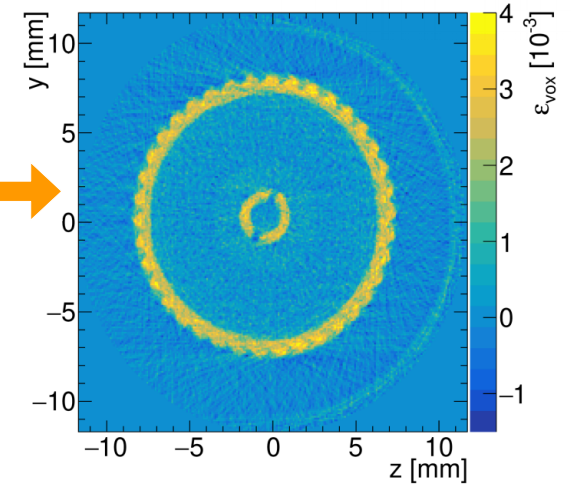
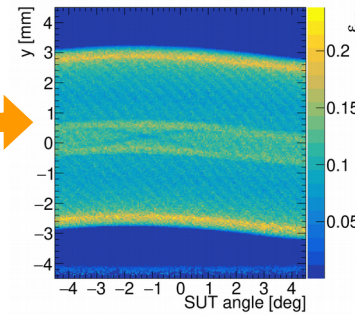
2D Material Budget map



Vert. slice



Sinogram

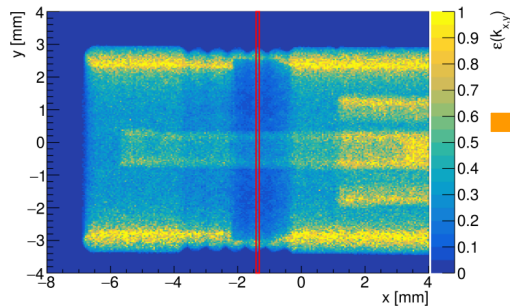


Examples of 3D MBI

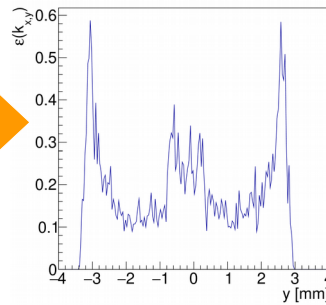


Reconstruction

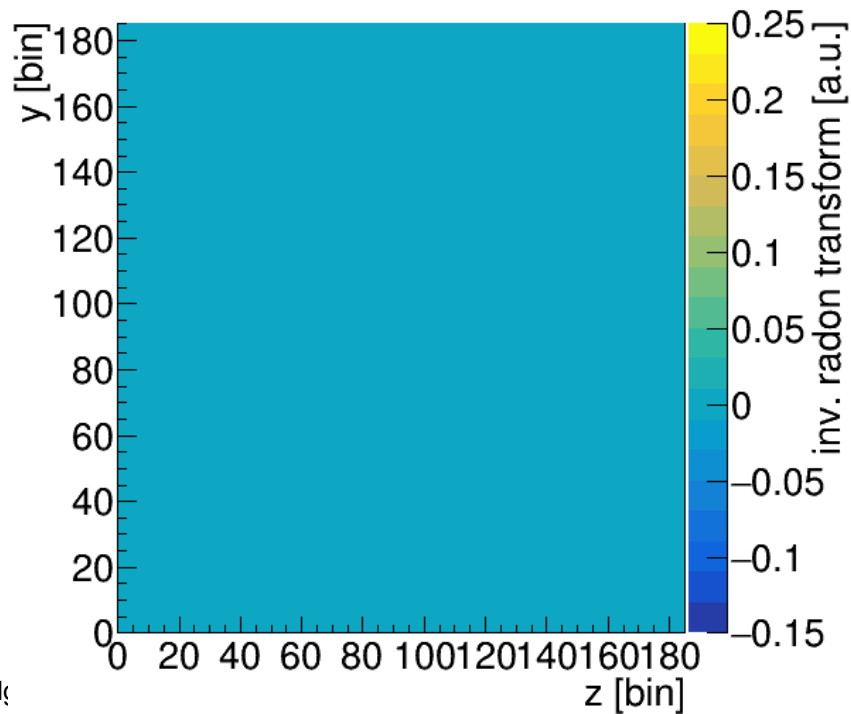
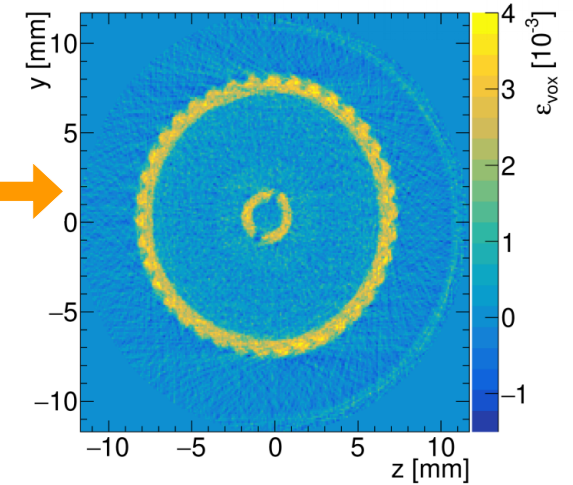
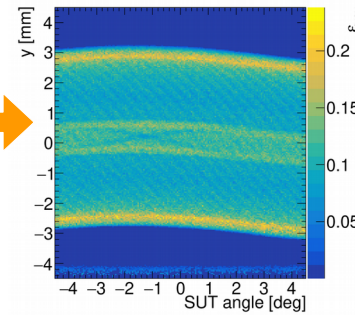
2D Material Budget map



Vert. slice



Sinogram

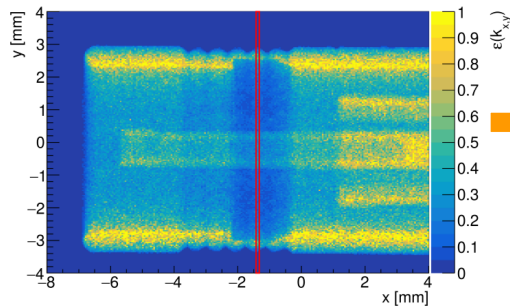


Examples of 3D MBI

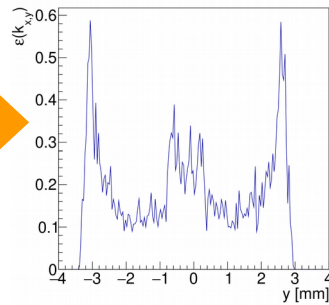


Reconstruction

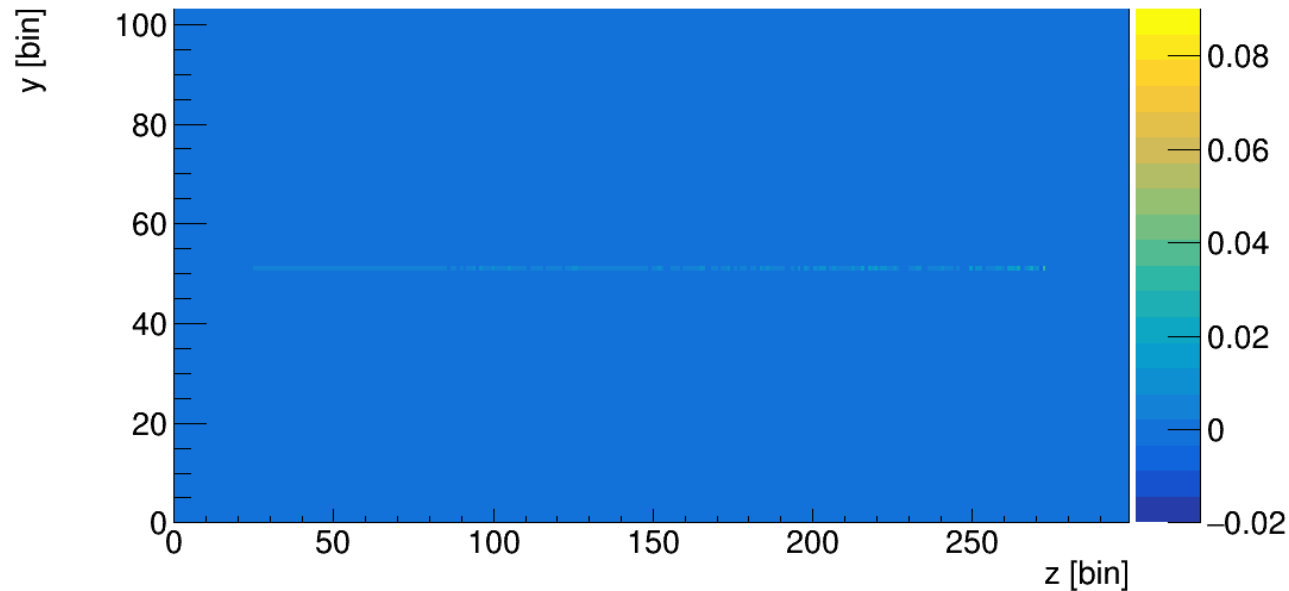
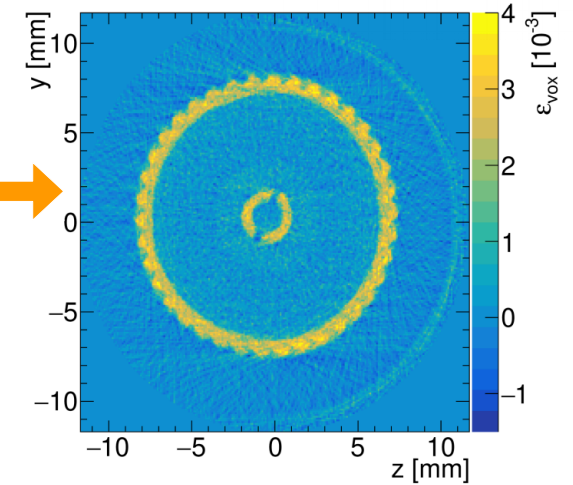
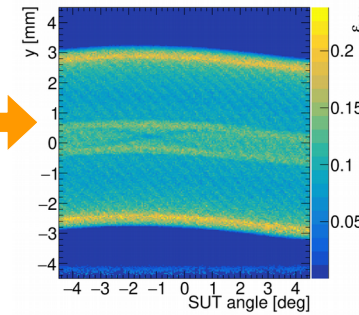
2D Material Budget map



Vert. slice

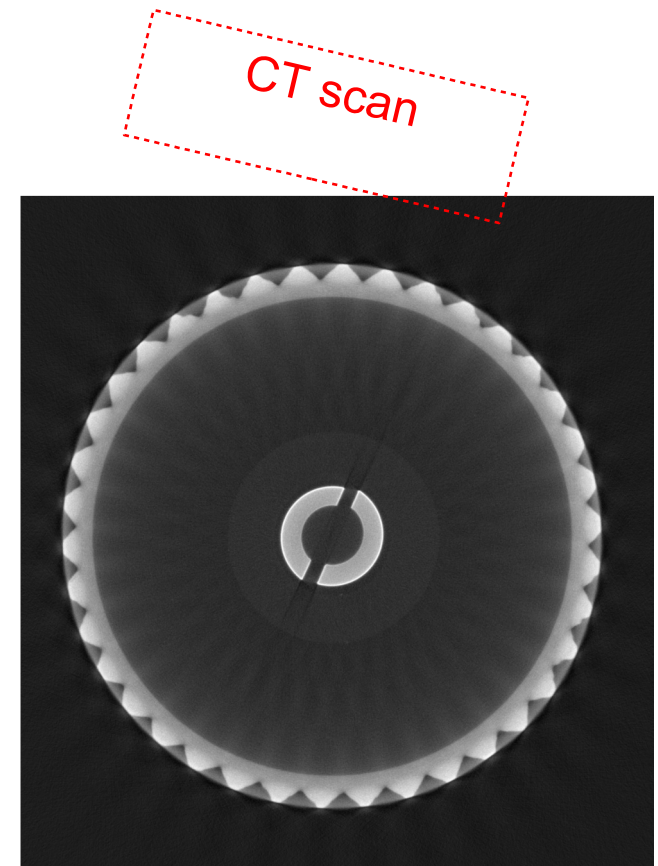
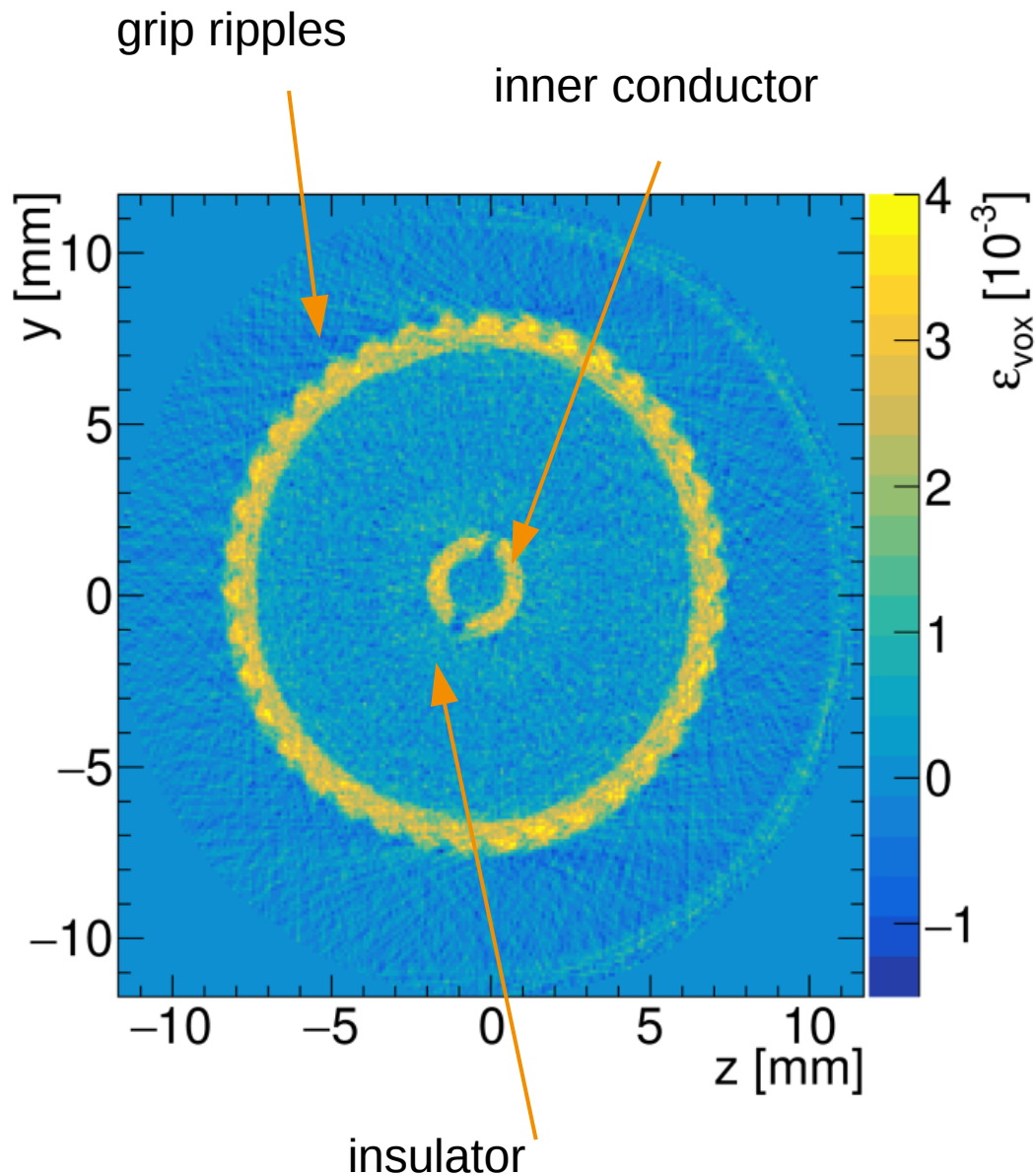


Sinogram



inv. radon transform [a.u.]

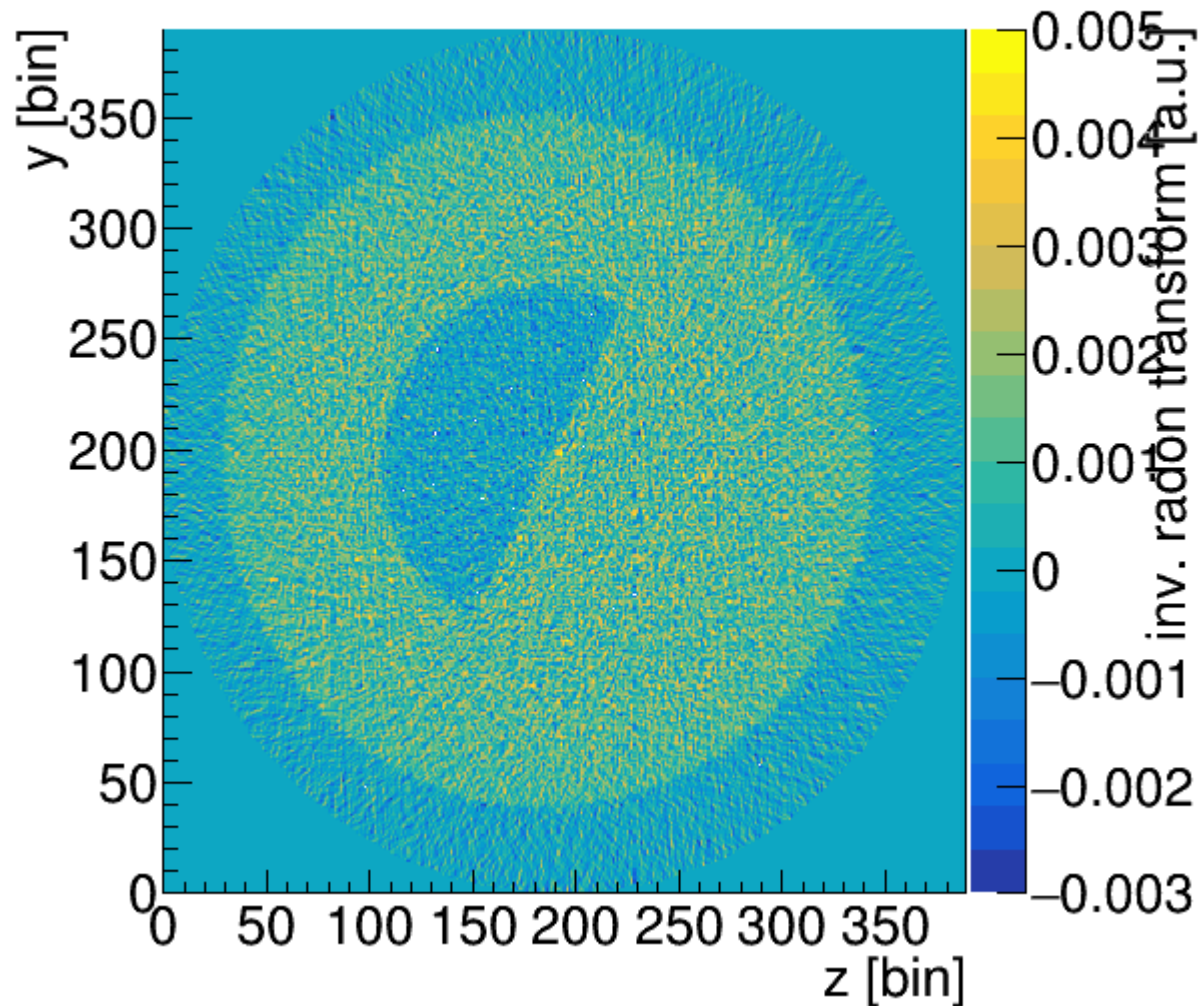
Comparison to CT



**Helmholtz-Zentrum
Geesthacht**
Zentrum für Material- und Küstenforschung

Example of 3D MBI

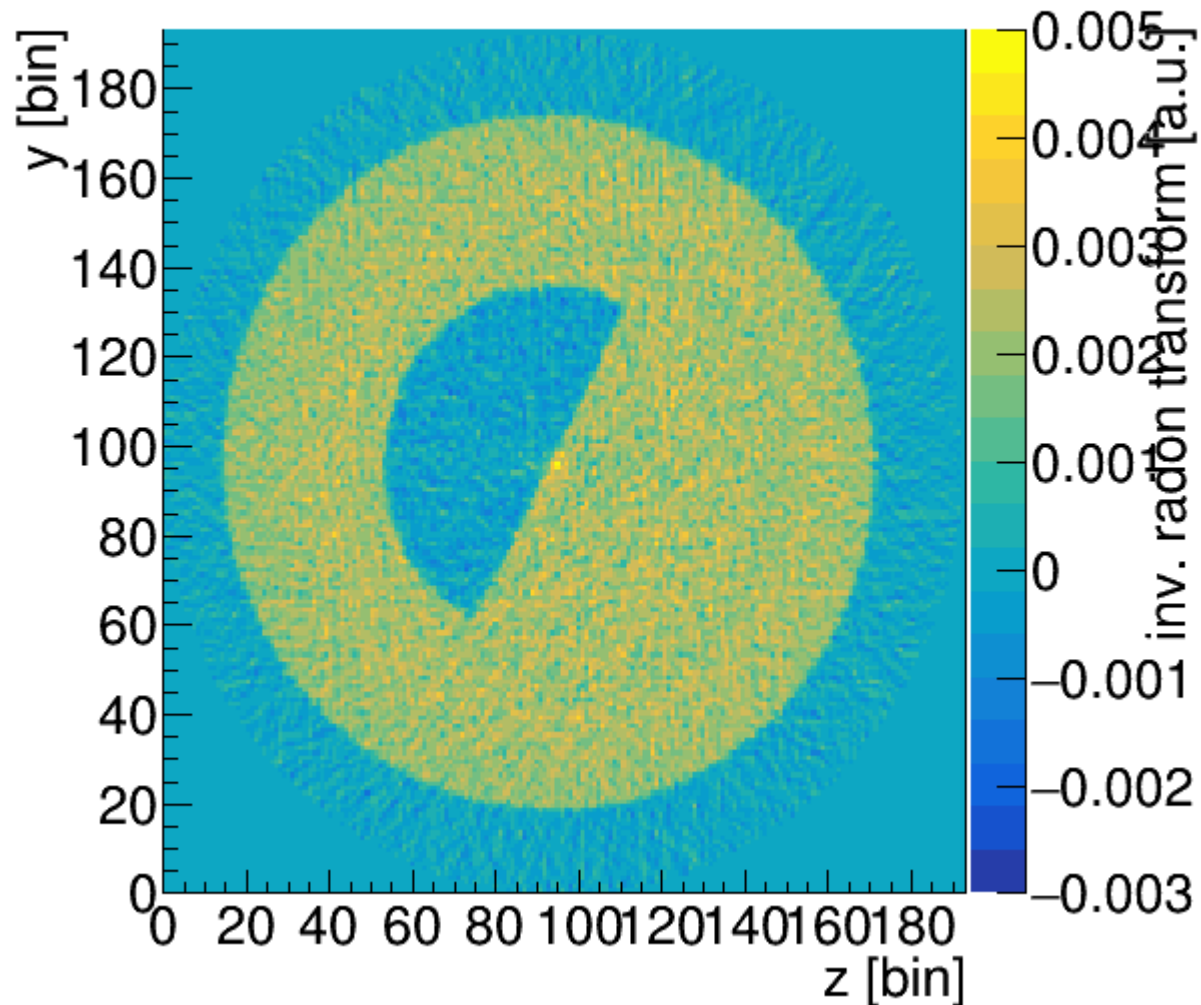
50 um voxel



16 mm diameter
3D printed nickel

Example of 3D MBI

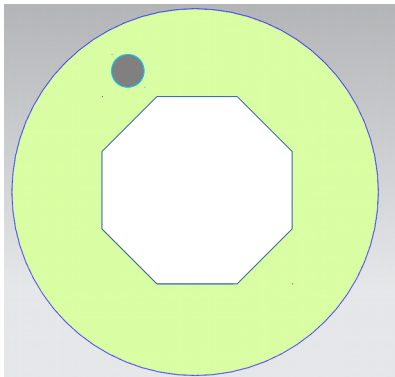
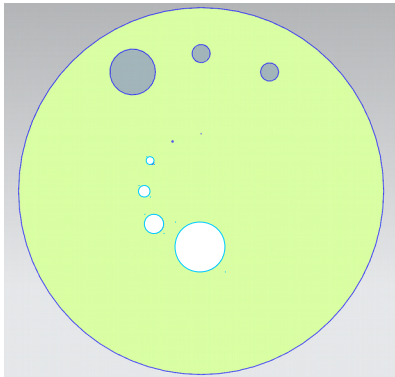
100 um voxel



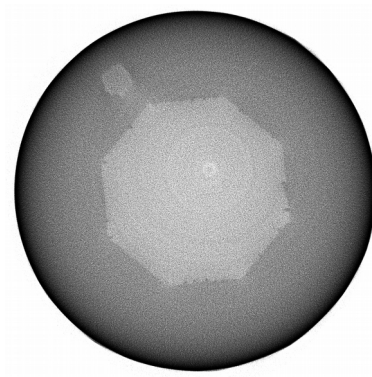
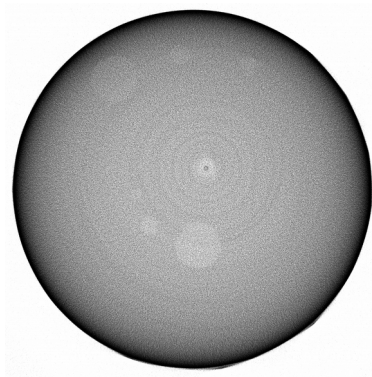
16 mm diameter
3D printed nickel

Comparison to CT

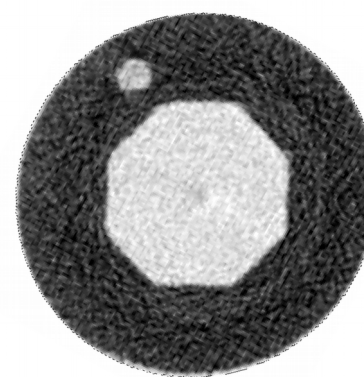
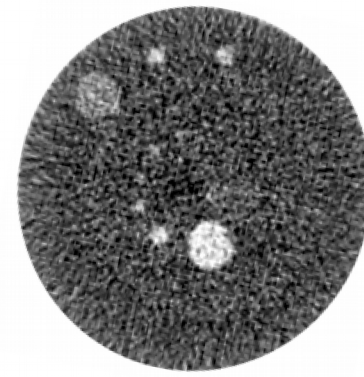
Cross-sections



**CT scan at 170 kVp
(inverted grey scale)**

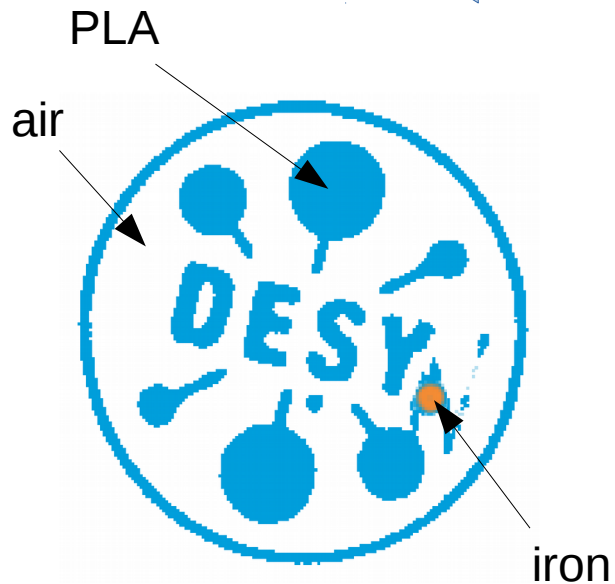
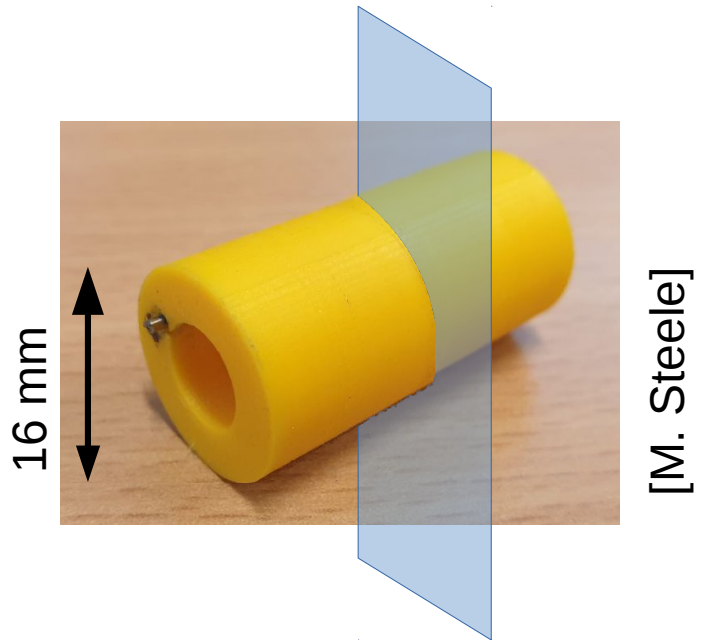


MBI

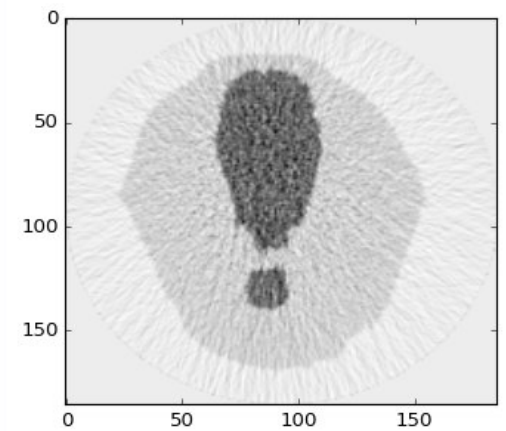
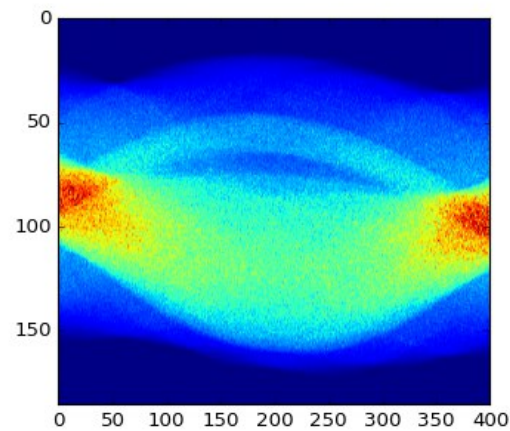
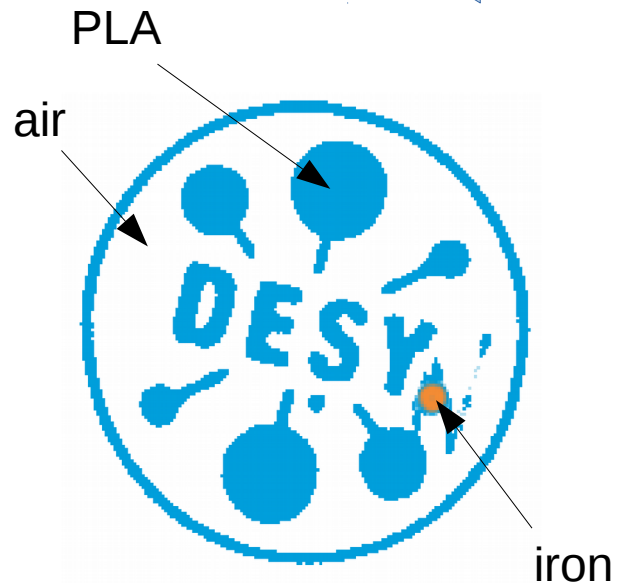
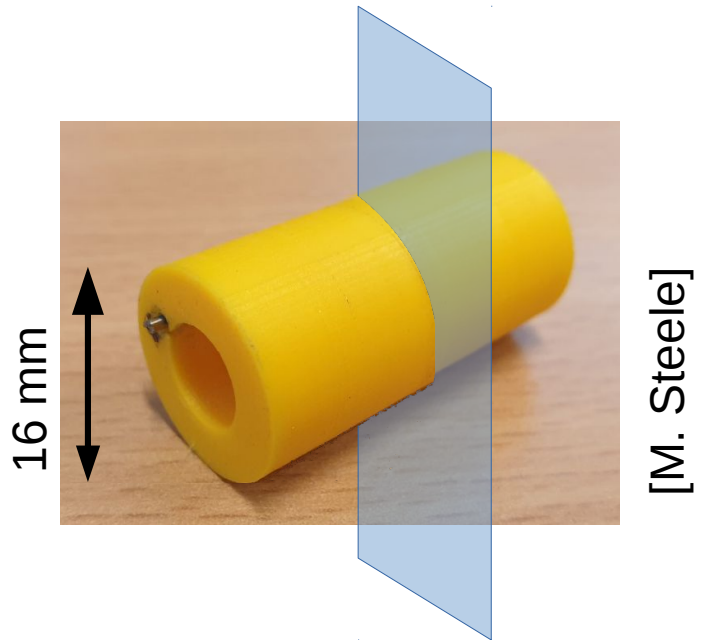


 **Helmholtz-Zentrum
Geesthacht**
Zentrum für Material- und Küstenforschung

Tissue-like samples, 500 MeV



Tissue-like samples, 500 MeV



Conclusion

- MBI works up to at least $\varepsilon = 100\%$ (human's head $\sim 80\%$)
- Voxel size limited to $\sim 10 \mu\text{m}$
practical limit is rate dependent $\rightarrow 50 \mu\text{m}$ @ DESY
- Started at 2 GeV, reached 500 MeV easily (method-wise)
- Multitude of samples tested

Outlook

- Calibration curves for tissue-equivalent materials
(Summer student)
- Improve image reconstruction (PD position open)
- Estimate CNR a.f.o. dose (particles per pixel per projection)
- Understand clinical needs (CNR, resolution) and dose limits
- Investigate market potential

Contrast vs Resolution

